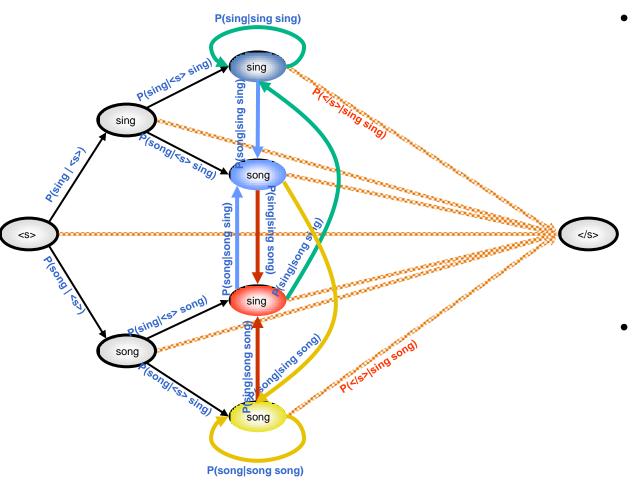


Design and Implementation of Speech Recognition Systems

Spring 2013

Class 26: Exact and Inexact Search 24 Apr 2013

Representing N-gram LMs as graphs



- For recognition, the N-gram LM can be represented as a finite state graph
 - Recognition can be performed exactly as we would perform recognition with grammars
- Problem: This graph can get enormously large
 - There is an arc for every single N-gram probability!
 - Also for every single N-1, N-2 .. 1-gramprobabilities

The representation is wasteful

- In a typical N-gram LM, the vast majority of bigrams, trigrams (and higher-order N-grams) are computed by backoff
 - They are not seen in training data, however large it may be

$$P(w | w_a w_b w_c) = backoff(w_a w_b w_c) P(w | w_b w_c)$$

- The backed-off probability for an N-gram is obtained from the N-1 gram!
- So for N-grams computed by backoff it should be sufficient to store only the N-1 gram in the graph
 - Only have arcs for $P(w \mid w_b w_c)$; not necessary to have explicit arcs for $P(w \mid w_a w_b w_c)$
 - This will reduce the size of the graph greatly

Ngram LM as FSG: accounting for backoff

- N-Gram language models with back-off can be represented as finite state grammars
 - That explicitly account for backoff!
- This also permits us to use grammar-based recognizers to perform recognition with Ngram LMs
- There are a few precautions to take, however

Ngram to FSG conversion: Trigram LM

• \1-grams:

```
-1.2041 <UNK> 0.0000

-1.2041 </s> 0.0000

-1.2041 <s> -0.2730

-0.4260 one -0.5283

-1.2041 three -0.2730

-0.4260 two -0.5283
```

• \2-grams:

```
-0.1761 <s> one 0.0000

-0.4771 one three 0.1761

-0.3010 one two 0.3010

-0.1761 three two 0.0000

-0.3010 two one 0.3010

-0.4771 two three 0.1761
```

• \3-grams:

-0.3010 <s> one two
-0.3010 one three two
-0.4771 one two one
-0.4771 one two three
-0.3010 three two one
-0.4771 two one three
-0.4771 two one two
-0.3010 two three two

Step1: Add Explicit Ngrams:

♦ \1-grams:

-1.2041	<unk></unk>	0.0000
-1.2041		0.0000
-1.2041	<s> -0.2730</s>	
-0.4260	one -0.5283	
-1.2041	three	-0.2730
-0.4260	two -0.5283	

♦ \2-grams:

-0.1761	<s> one</s>	0.0000
-0.4771	one three	0.1761
-0.3010	one two	0.3010
-0.1761	three two	0.0000
-0.3010	two one	0.3010
-0.4771	two three	0.1761

♦ \3-grams:

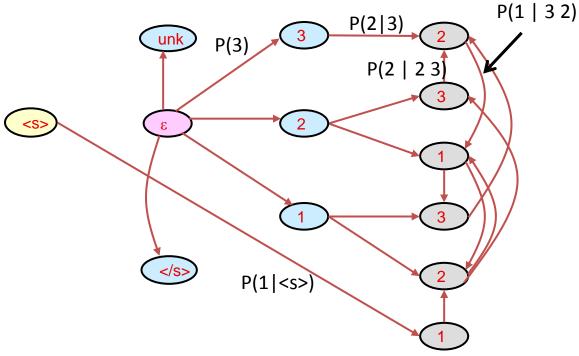
-0.3010	<s></s>	one	tw	70
-0.3010	one	thre	e	two
-0.4771	one	two	or	e
-0.4771	one	two	th	ree
-0.3010	thre	e tv	70	one
-0.4771	two	one	th	ree
-0.4771	two	one	tw	70
-0.3010	two	thre	ee	two

history level history level

P(212)

UG word

BG word



Note: The two-word history out of every node in the bigram word history level is unique

Note "EPSILON" Node for Unigram Probs

Step2: Add Backoffs

♦ \1-grams:

-1.2041	<unk></unk>	0.0000
-1.2041		0.0000
-1.2041	<s> -0.2730</s>	
-0.4260	one -0.5283	
-1.2041	three	-0.2730
-0.4260	two -0.5283	

♦ \2-grams:

-0.1761	<s> one</s>	0.0000
-0.4771	one three	0.1761
-0.3010	one two	0.3010
-0.1761	three two	0.0000
-0.3010	two one	0.3010
-0.4771	two three	0.1761

♦ \3-grams:

- -0.3010 <s> one two
 -0.3010 one three two
 -0.4771 one two one
 -0.4771 one two three
 -0.3010 three two one
 -0.4771 two one three
 -0.4771 two one two
 -0.3010 two three two
- From any node representing a word history "w_a" (unigram) add BO arc to epsilon
 - With score Backoff(w_a)
- From any node representing a word history " $w_a w_b$ " add a BO arc to w_b

BO(3)

unk

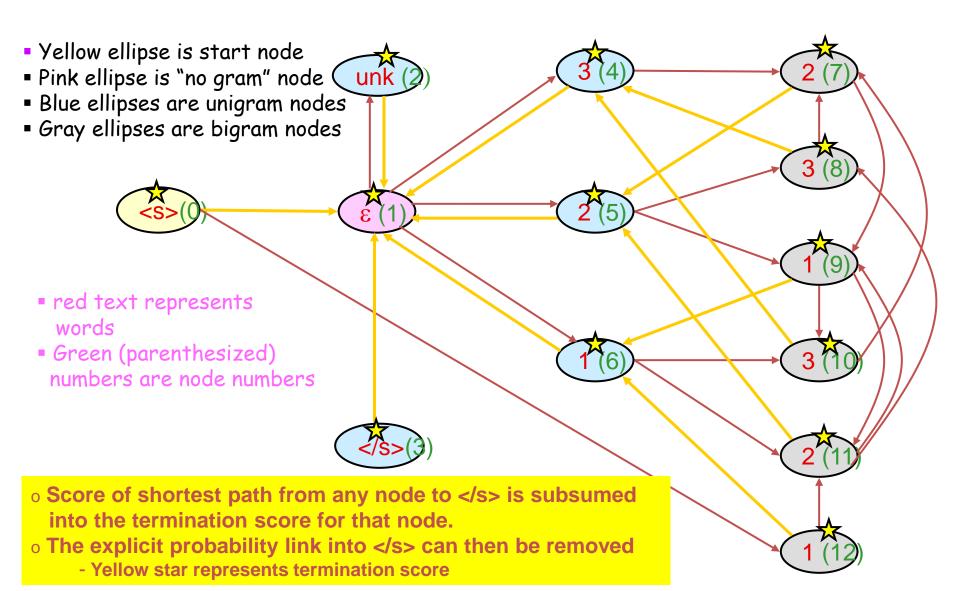
BO(3 2)

BO(2 3)

BO(13)

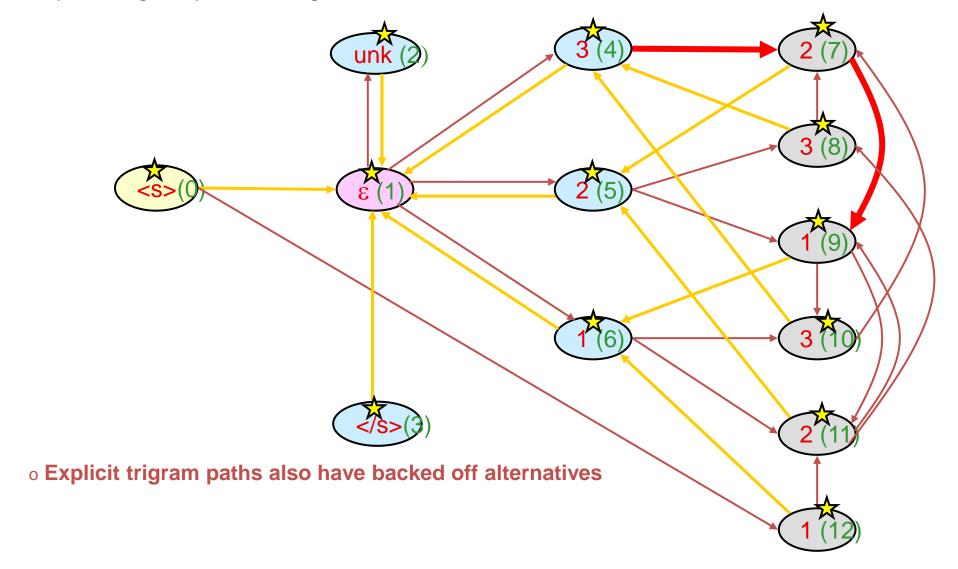
With score Backoff (w_a w_b)

Ngram to FSG conversion: FSG



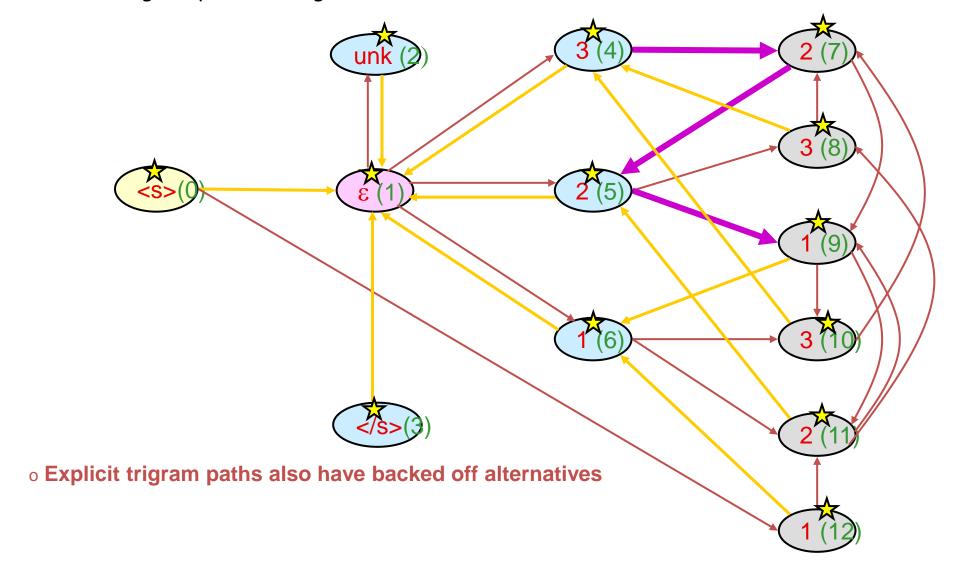
A Problem: Paths are Duplicated

Explicit trigram path for trigram "three two one"



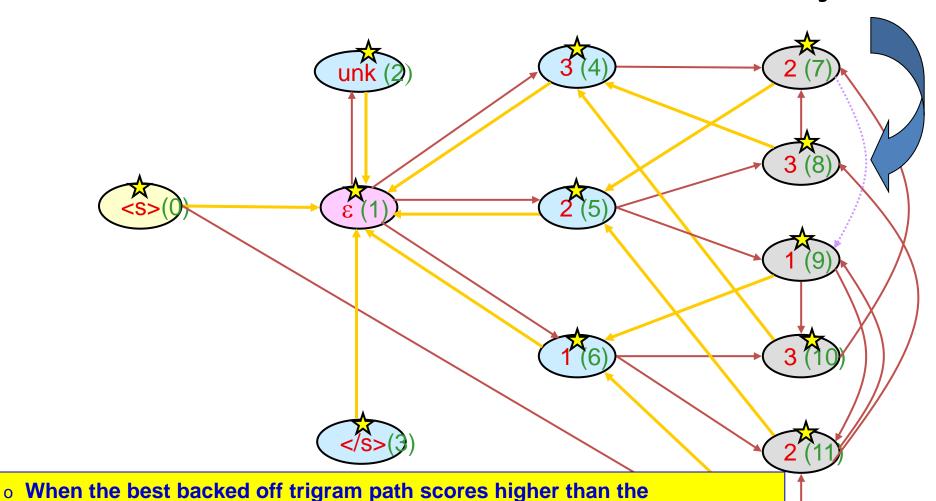
Backoff paths exist for explicit Ngrams

Backoff trigram path for trigram "three two one"



Delete "losing" edges

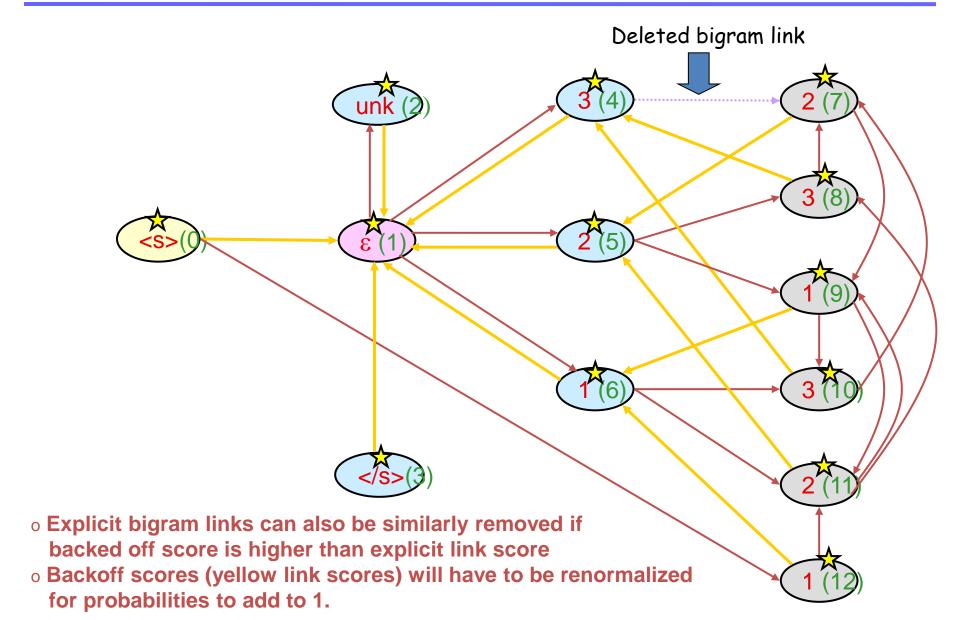
Deleted trigram link



Renormalization of backoff scores will be required to ensure sum(prob)=1

explicit trigram path, the explicit trigram link can be removed

Delete "Losing" Edges



Overall procedure for recognition with an Ngram language model

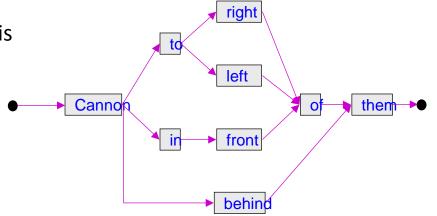
- Train HMMs for the acoustic model
- Train N-gram LM with backoff from training data

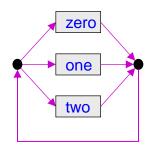
Overall procedure for recognition with an Ngram language model

- Construct the Language graph, and from it the language HMM
 - Represent the Ngram language model structure as a compacted N-gram graph, as shown earlier
 - The graph must be dynamically constructed during recognition – it is usually too large to build statically
 - Probabilities on demand: Cannot explicitly store all K^N
 probabilities in the graph, and comput them on the fly
 - K is the vocabulary size
 - Other, more compact structures, such as FSAs can also be used to represent the language graph
- Recognize

Types of "Language Models"

- Finite state grammars
 - The set of all possible word sequences is represented as a graph
- Context free grammars
 - A set of context-free rules:
 - Digit := 0 | 1 | 2;
 - Number = Digit | Number Digit;
 - Typically converted into a finite state graph for recognition
 - Graph may be approximate
 - Some CFGs cannot be represented as finitestate Graphs; require push-down automata
- N-gram language models

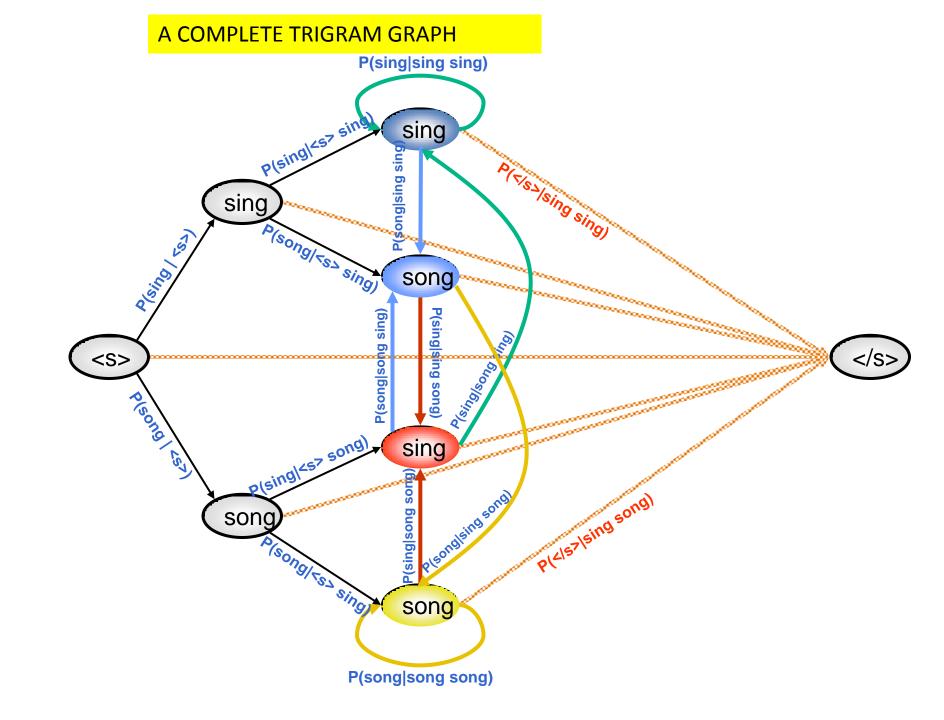




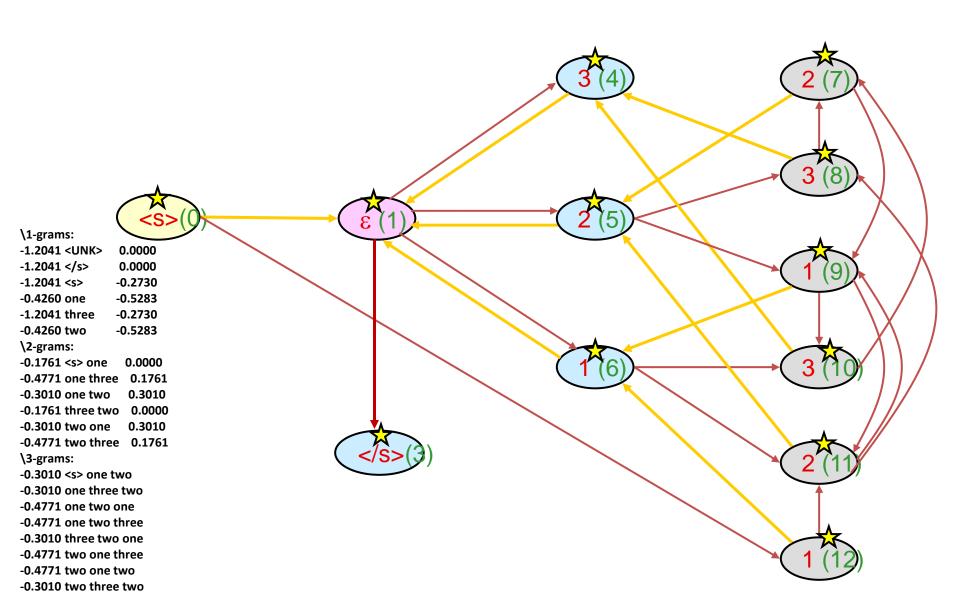
An Example Backoff Trigram LM

\1-grams: -1.2041 <UNK> 0.0000 -1.2041 </s> 0.0000 -1.2041 <s> -0.2730 -0.4260 one -0.5283 -1.2041 three -0.2730 -0.4260 two -0.5283 \2-grams: -0.1761 <s> one 0.0000 -0.4771 one three 0.1761 -0.3010 one two 0.3010 -0.1761 three two 0.0000 -0.3010 two one 0.3010 -0.4771 two three 0.1761 **\3-grams:** -0.3010 <s> one two -0.3010 one three two -0.4771 one two one **-0.4771** one two three -0.3010 three two one -0.4771 two one three -0.4771 two one two

-0.3010 two three two



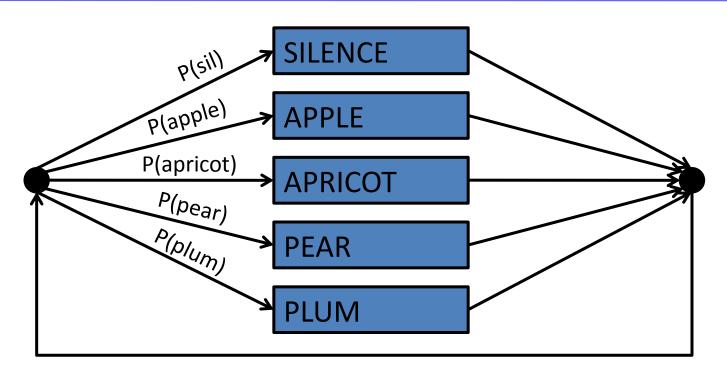
A "Reduced" Trigram Graph



Ngrams: Can we do better

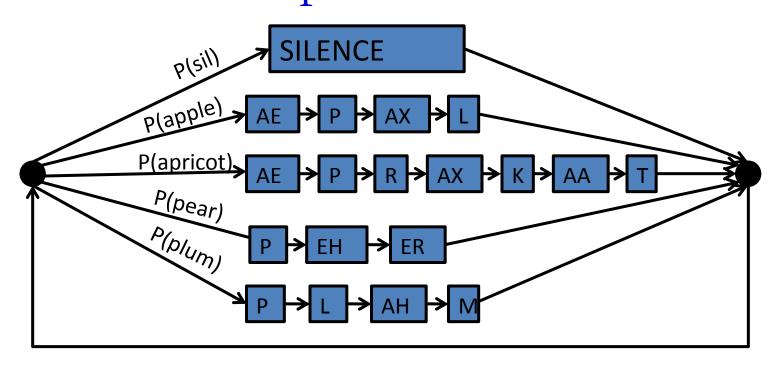
- Even reduced graphs can get very large
 - Rarely directly used for recognition
- Alternate strategies must be employed
 - Lextrees
 - For low-order Ngrams only
 - Approximate decoding strategies
 - Lextrees + approximate decoding strategies
- Minimization strategies
 - WFSTs: Using techniques from finite state automata theory

A Unigram Graph



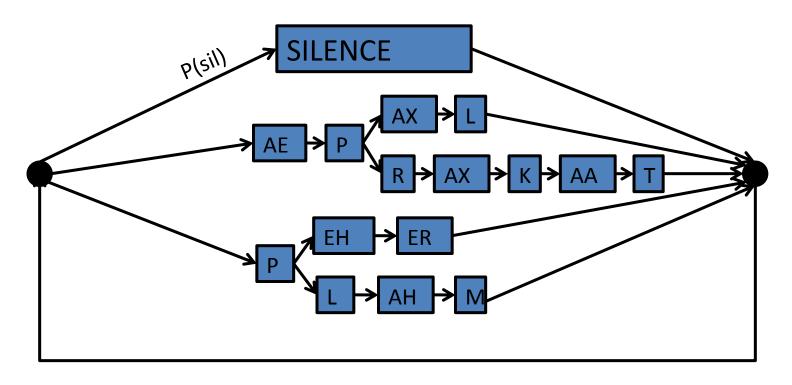
- Just a set of parallel word models with a loopback
- The ingoing edge into each word carries its LM probability

A Unigram Graph with words built from phonemes



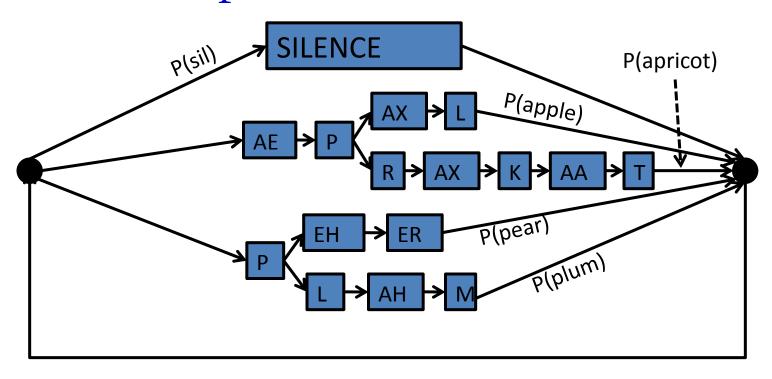
- Composing Word models from phoneme models
- Each rectangle is actually an HMM. The entire graph is a large HMM

A Unigram Lextree



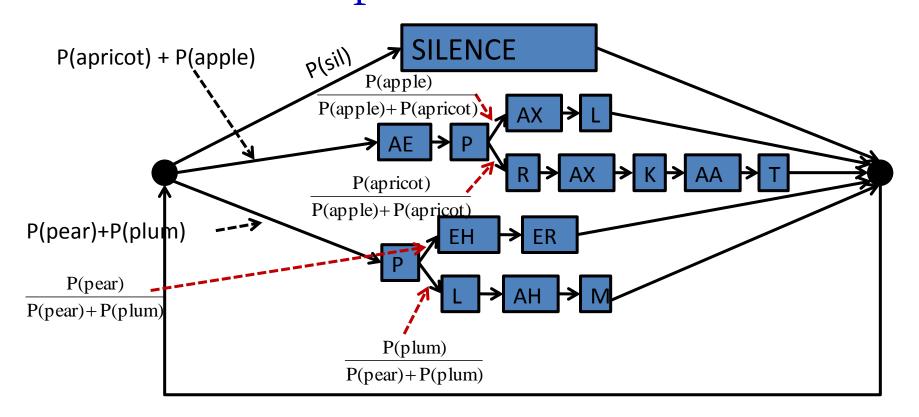
- Eliminate redundancy in the graph
- But where do word probabilities get introduced?
 - The identity of the word is not evident at entry!

A Unigram Lextree with trailing probabilities



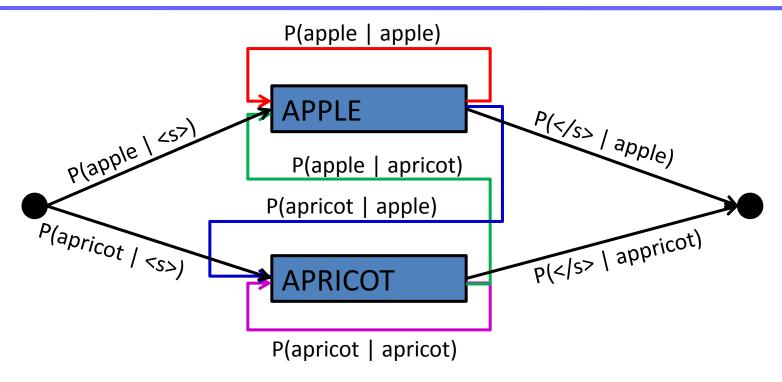
- Introduce word probabilities on the exit arcs
 - The word identity is evident at that point

A Unigram Lextree with spread probabilities



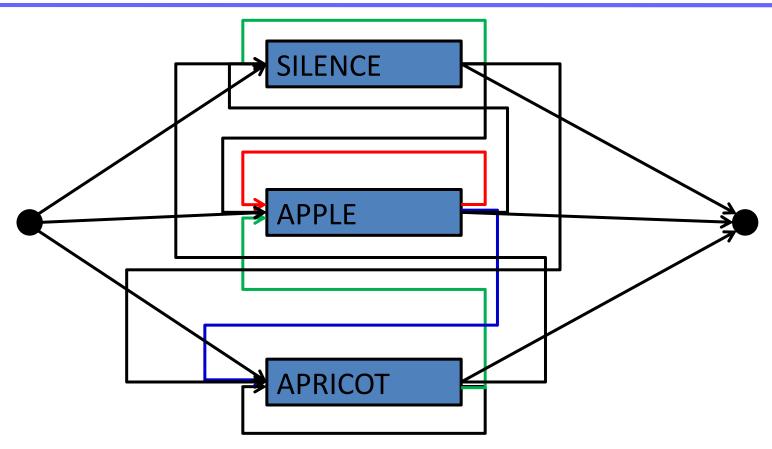
- Better still: Spread the probabilities
 - Any arc that first identifies a subset of words carries the conditional probability of that subset

A Bigram Graph



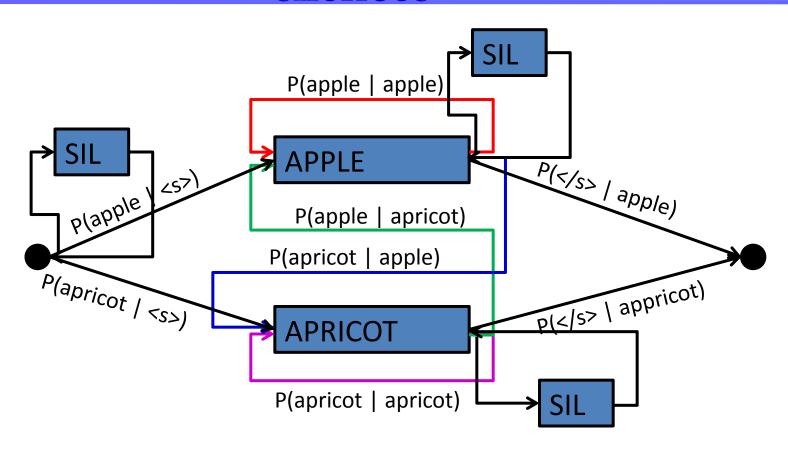
- Explicit connection from every word to every word
 - Connections carry bigram probabilities

A Bigram Graph: Adding silence



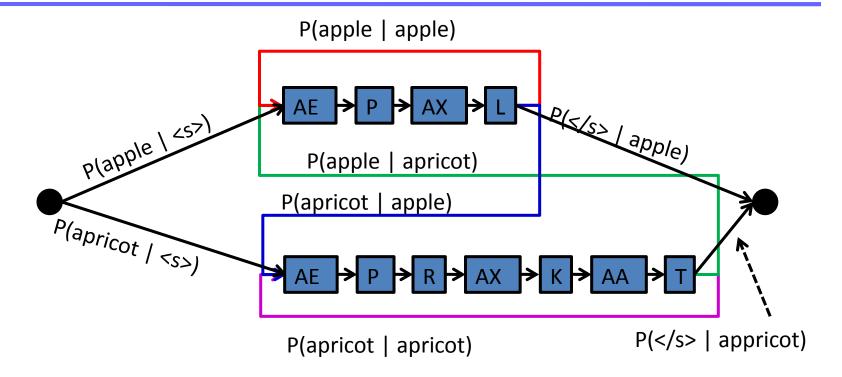
- Addition of looping silence is non-trivial
 - What is the probability on the outgoing edges from silence?
 - We do not have probabilities for P(word | silence), only P(word | word)
 - If a silence occurs between two words, we use the word before the silence as context

A Bigram Graph: Proper insertion of silences



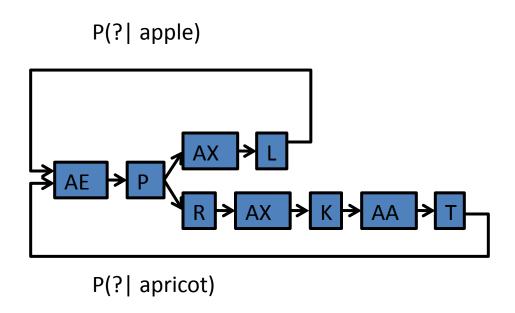
- An explicit silence model at the end of every word
 - We get an enormous number of copies of the silence model!

What about Lextrees



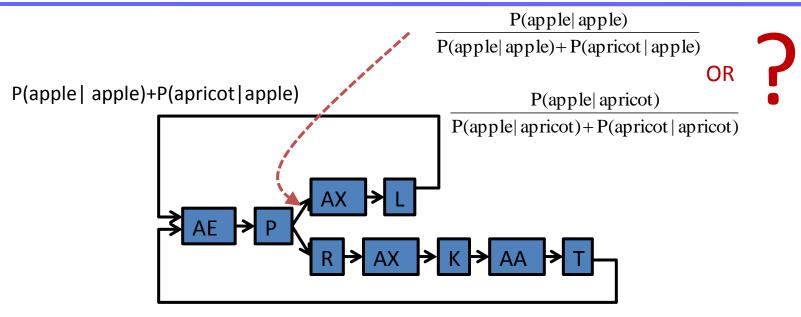
Can this be collapsed to a lextree?

Probabilities on lextrees



- Word identities are not known on entry
 - Only on word exit

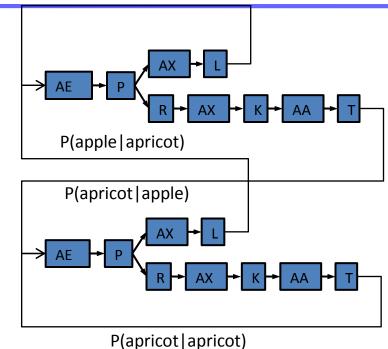
Probabilities on lextrees



P(apple | apricot)+P(apricot | apricot)

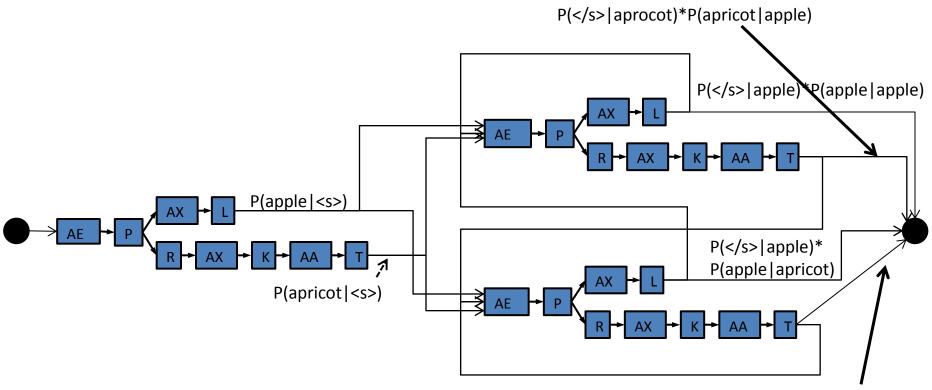
- Word identities are not known on entry
 - Only on word exit
- Word probabilities cannot be smeared
 - Both word histories lead into the same node
 - Uncertain which probability terms to use on inner connections

Correct Lextrees



- Each edge carries the bigram probability of the *exited* word
 - This is different from the "flat" structure where the edges carried probabilities of words to be entered
 - All "Apple" exits enter lextree 1, all "apricot" exits enter lextree 2
- This graph is not complete: it ignores the first word in a sentence

Correct full lextrees

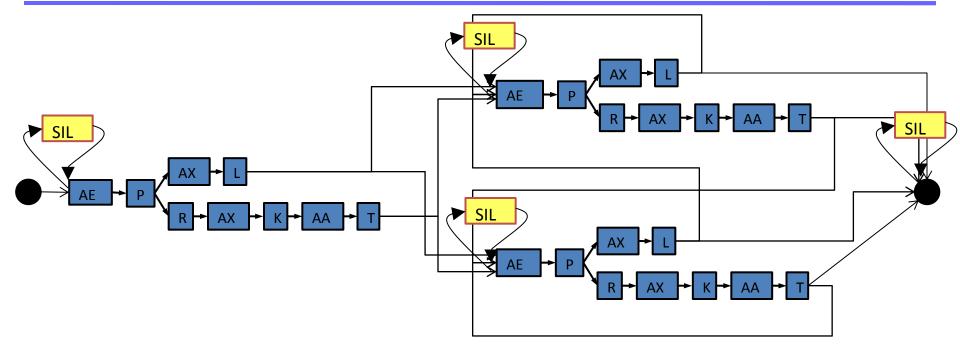


The word entry bigrams need their own lextree!

P(</s>|apricot)*p(apricot|apricot)

- Since neither of the second-level lextrees can represent a sentence-beginning context
 - Lextree 1 represents the "Apple" context (only exits from the word "apple" enter this lextree
 - Lextree 2 is the "apricot" context
- Why do transitions into the end of sentence have products of two probability terms?

Correct full lextrees with silence



- Fortunately, adding silence doesn't complicate this too much
- Add a looping silence at the beginning of each lextree
 - And one at the sentence terminator

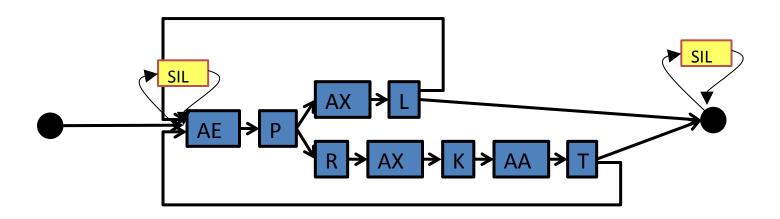
Correct Structures are Limiting

- The "correct" flat N-gram structure can get very large
 - D + D² + .. + D^{N-1} word HMMs are required in the larger "Language" HMM
- Even the reduced N-gram structure can be very large
 - Reduced structures are not exact
 - Multiple paths exist for each N-gram
 - Reduced structures are nevertheless used very effectively by WFST-based strategies
- Lextrees result in significant compression for Unigram LMs
- But for N-gram LMs "correct" Lextree-based graphs are much larger than "flat" graphs
 - Need D + D^2 + .. + D^{N-1} lextrees!!

Approximate Search Strategies

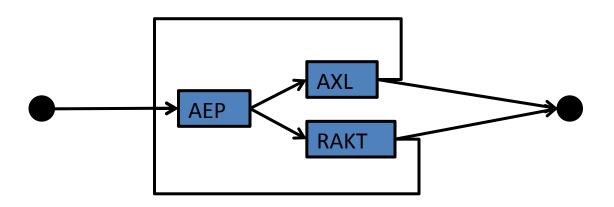
- Approximate search strategies are not guaranteed to result in the best recognition
 - Although, in practice they often approach the optimal recognition
- Efficiency is obtained by dynamically modifying graph parameters
 - I.e. language probabilities in the language HMM
- This is typically done by utilizing word histories
 - From a backpointer table
- The resulting improvement in efficiency can be very large

Approximate search with a Unigram Lextree



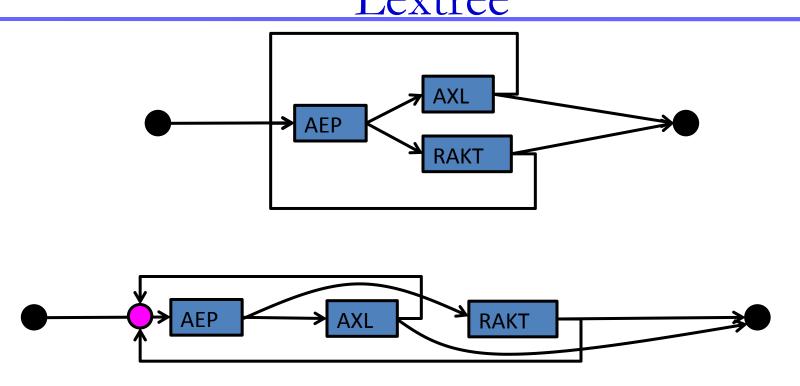
- Utilize the above lextree as the basic HMM structure
 - Note no language model probabilities are loaded on the lextree
 - These will be imposed dynamically during search
 - In practice unigram probabilities may be factored into the lextree and factored out during search
 - We will ignore this option in the following explanation

Approximate search with a Unigram Lextree

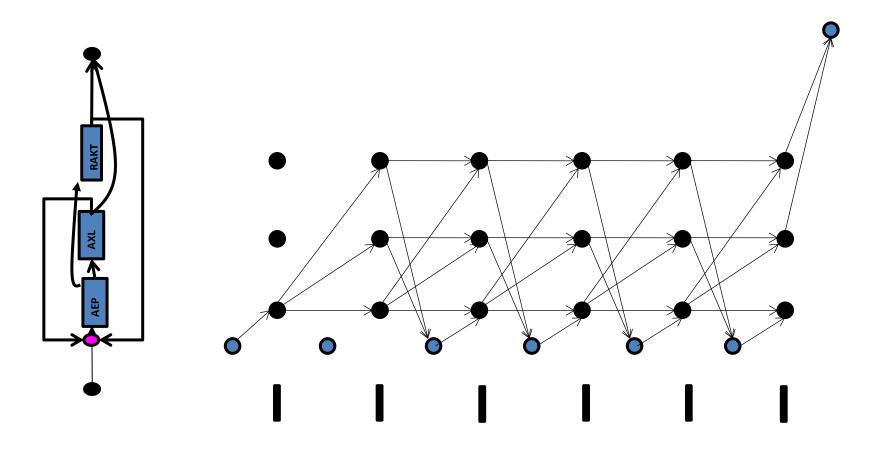


- We will use the simplified figure above in the following explanation
 - AEP is the concatenation of AE and P
 - AXL is the concatenation of AX and L
 - RAKT is the concatenation of R AX K AA and T
- Will not explicitly show silence models

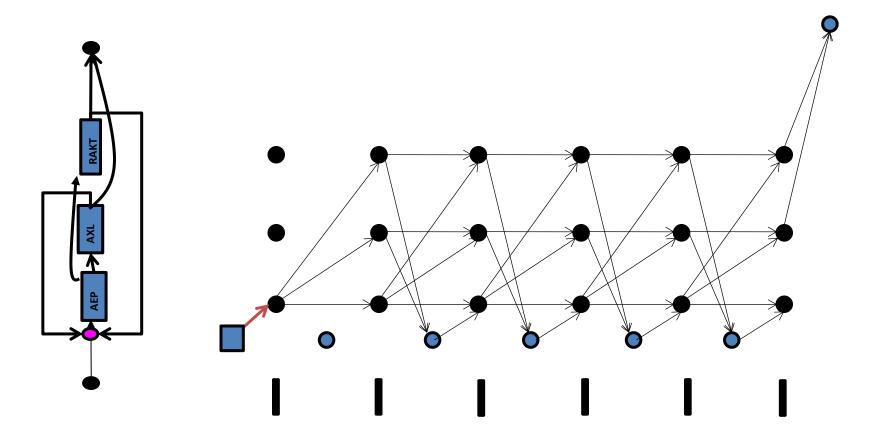
Approximate search with a Unigram Lextree



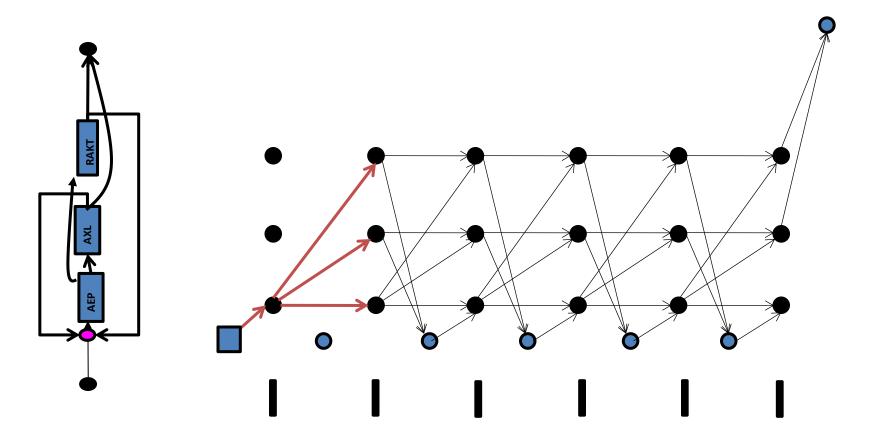
- A Linear Representation that is useful to draw a trellis
 - Note: Each box is actually an HMM (representing a sequence of phonemes)
 - For simplicity we will assume each box has only one state

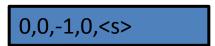


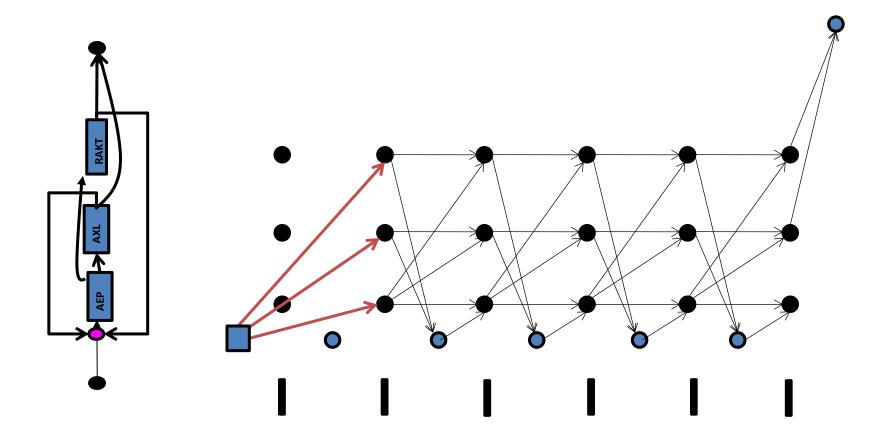
A normal unigram trellis, but with no LM probabilities at word transitions



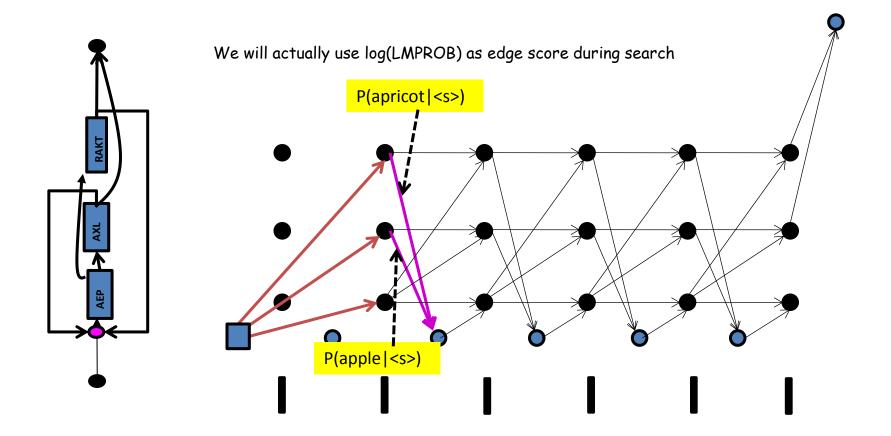
• A normal unigram trellis, but with no LM probabilities at word transitions



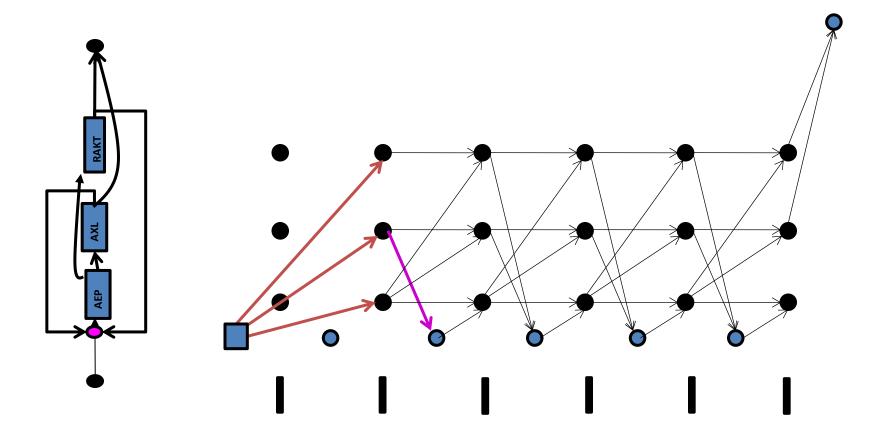






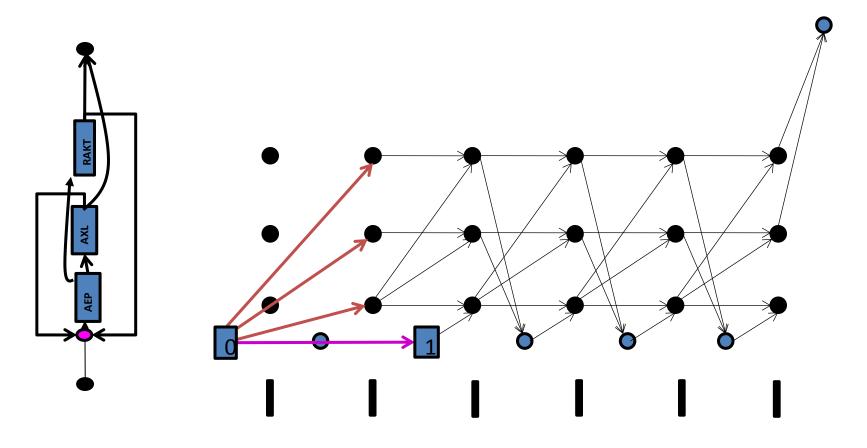






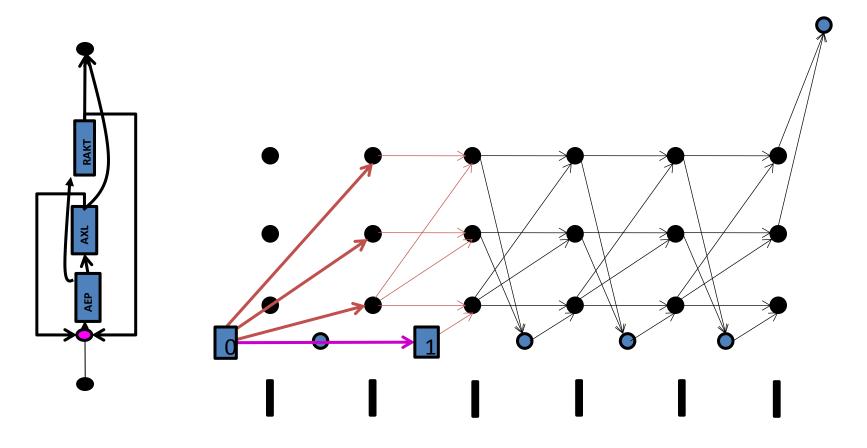
0,0,-1,0,<s>

1,1,s1,0,apple



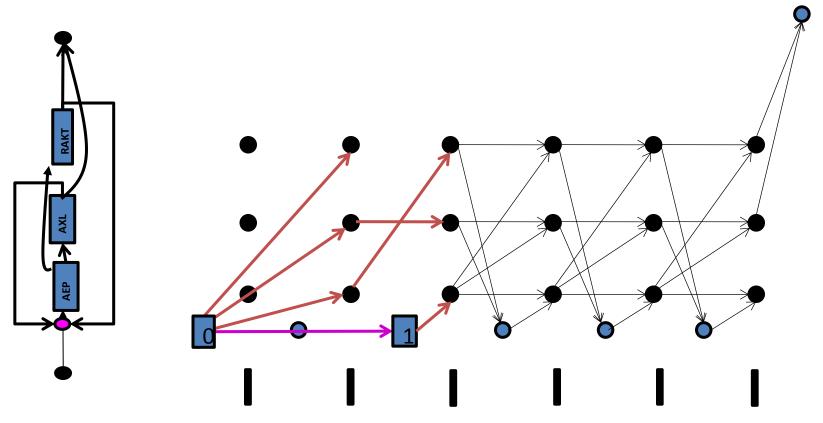
0,0,-1,0,<s>

1,1,s1,0,apple

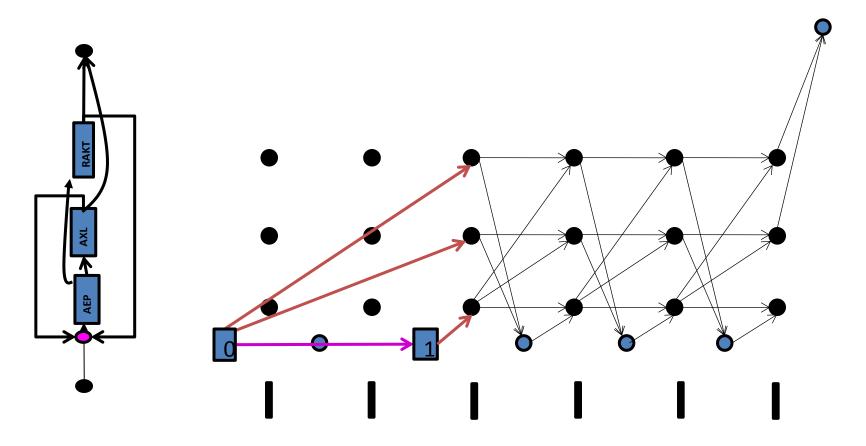


1,1,s1,0,apple

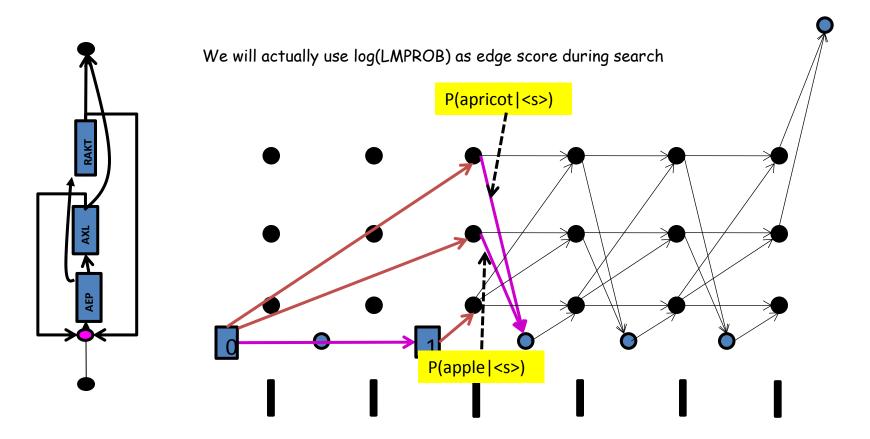




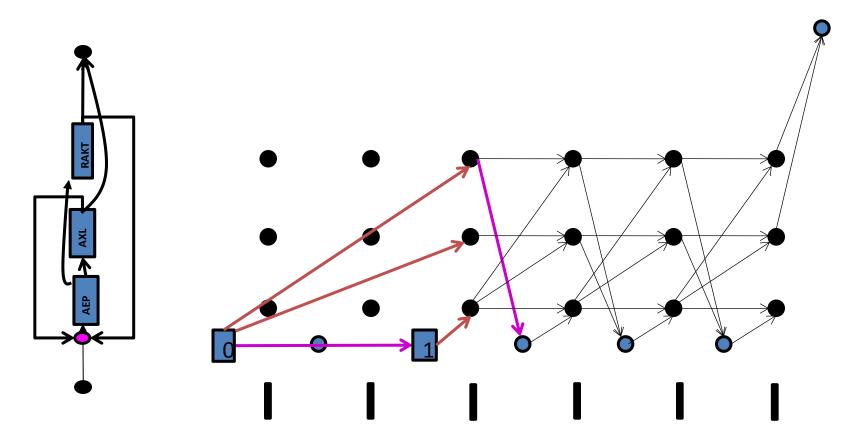
0,0,-1,0,<s>
1,1,s1,0,apple



0,0,-1,0,<s>
1,1,s1,0,apple



0,0,-1,0,<s>
1,1,s1,0,apple

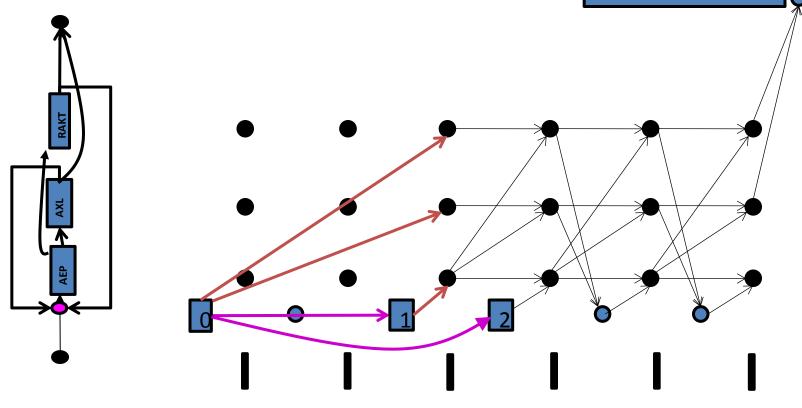


Id,time,parent,score,word

0,0,-1,0,<s>

1,1,s1,0,apple

2,2,s2,0,apricot

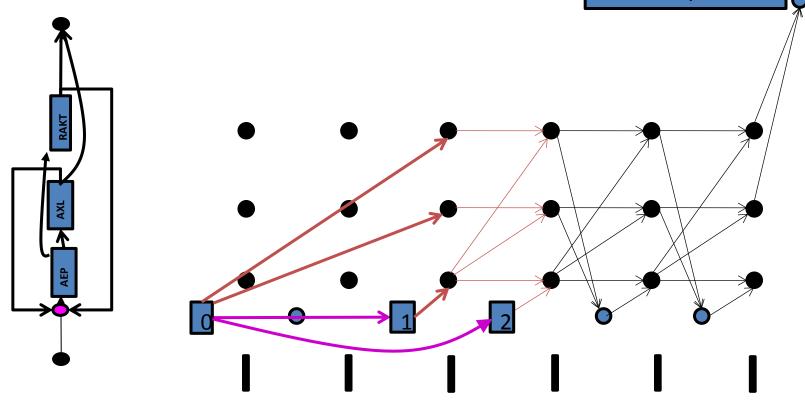


Id,time,parent,score,word

0,0,-1,0,<s>

1,1,s1,0,apple

2,2,s2,0,apricot

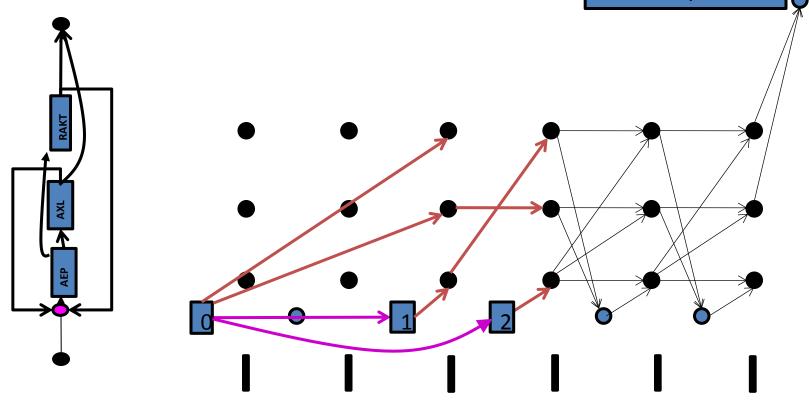


Id,time,parent,score,word

0,0,-1,0,<s>

1,1,s1,0,apple

2,2,s2,0,apricot

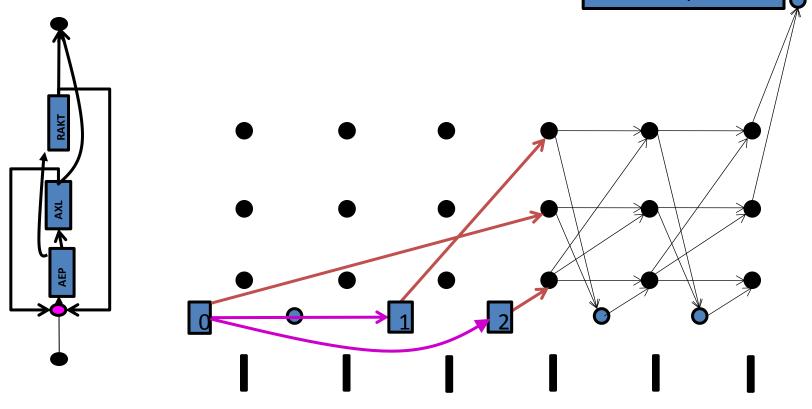


Id,time,parent,score,word

0,0,-1,0,<s>

1,1,s1,0,apple

2,2,s2,0,apricot

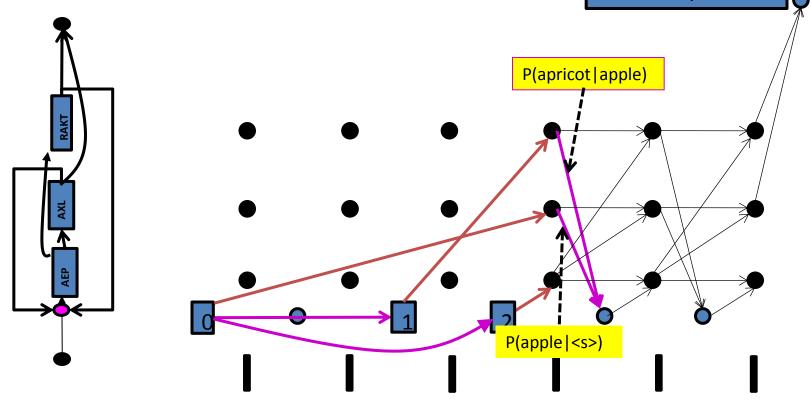


Id,time,parent,score,word

0,0,-1,0,<s>

1,1,s1,0,apple

2,2,s2,0,apricot



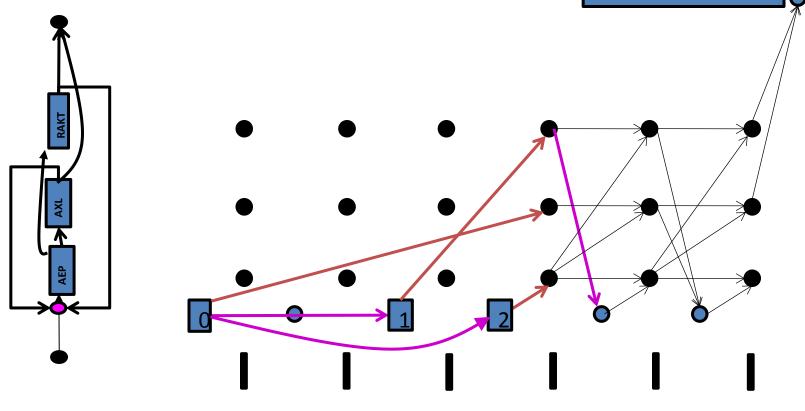
- The transition out of "Apricot" carries the probability P(Apricot|Apple) because the parent of the current state is the word "apple"
- This information is retrieved from the backpointer table

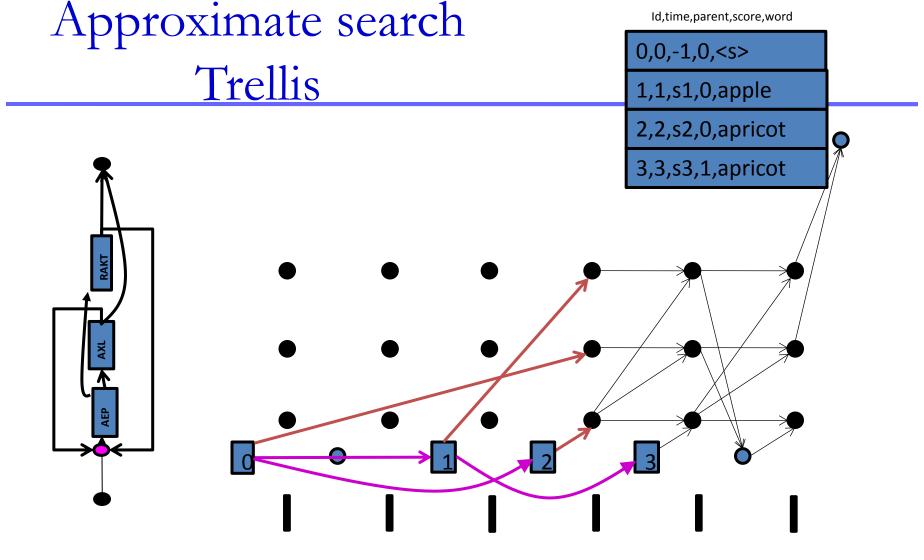
ld,time,parent,score,word

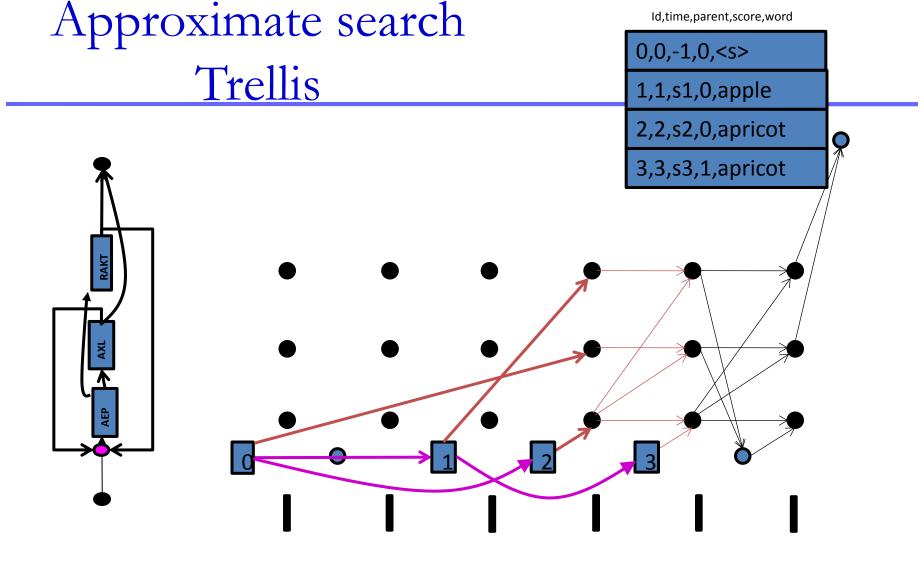
0,0,-1,0,<s>

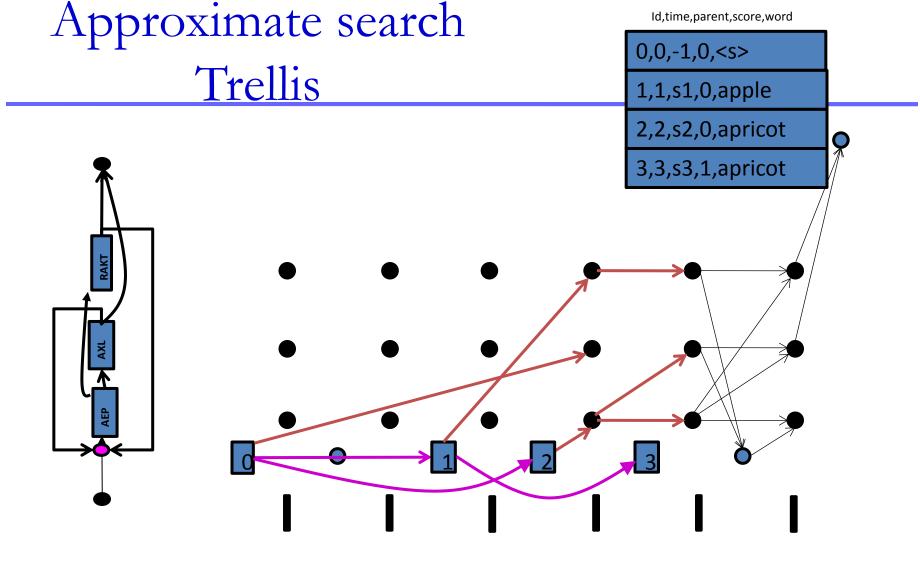
1,1,s1,0,apple

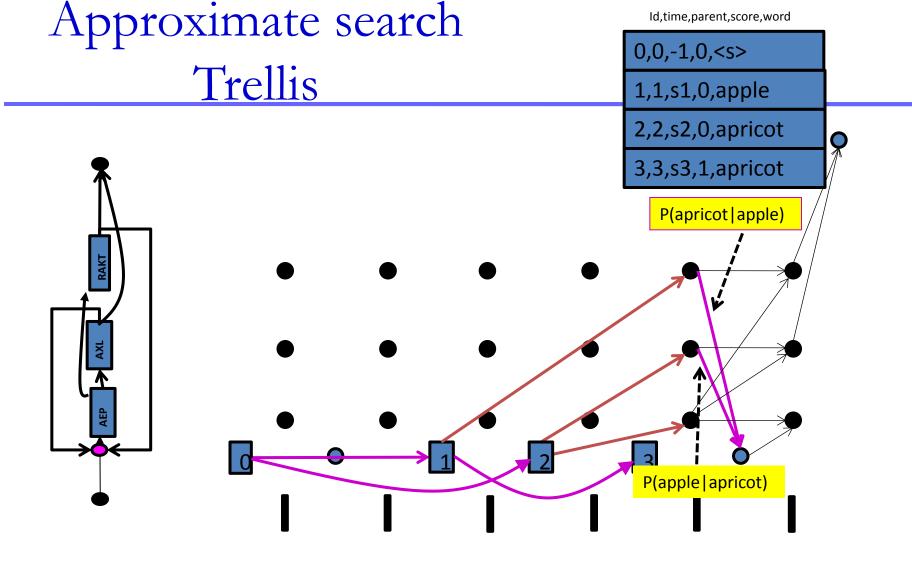
2,2,s2,0,apricot



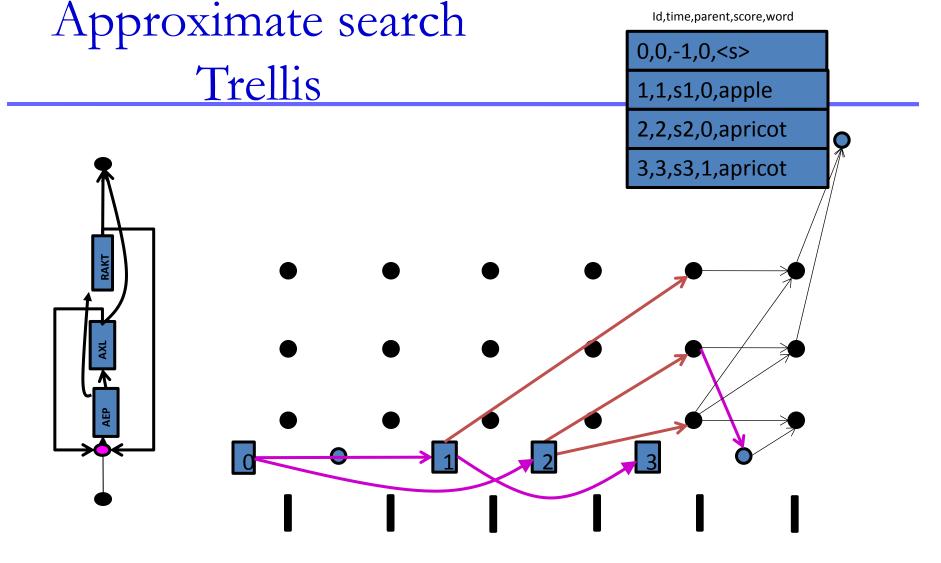




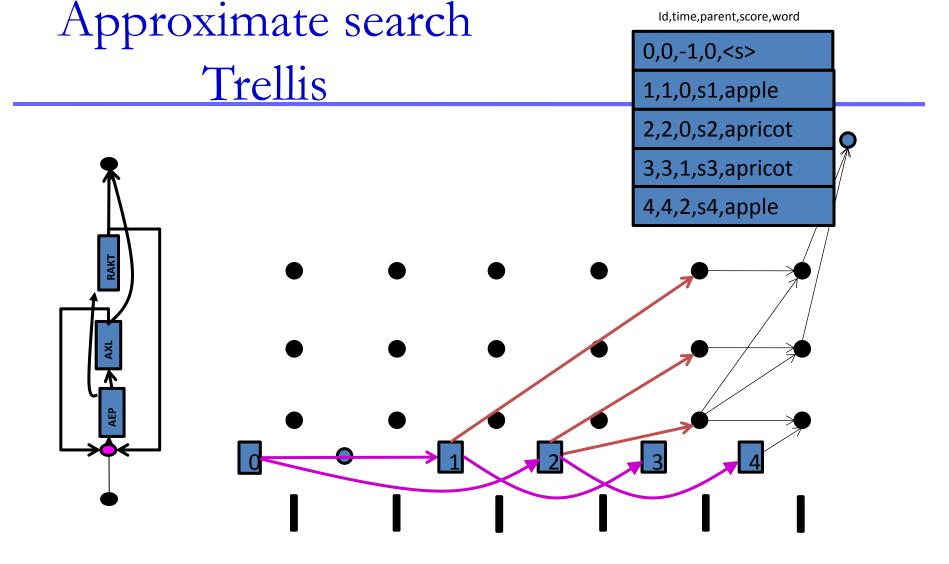




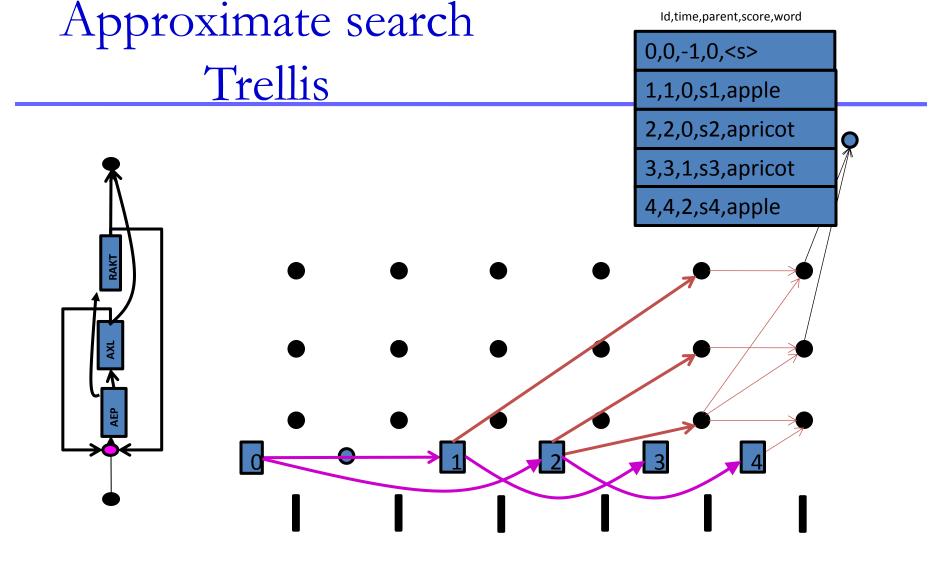
Note the conditioning word in the bigram probabilities applied



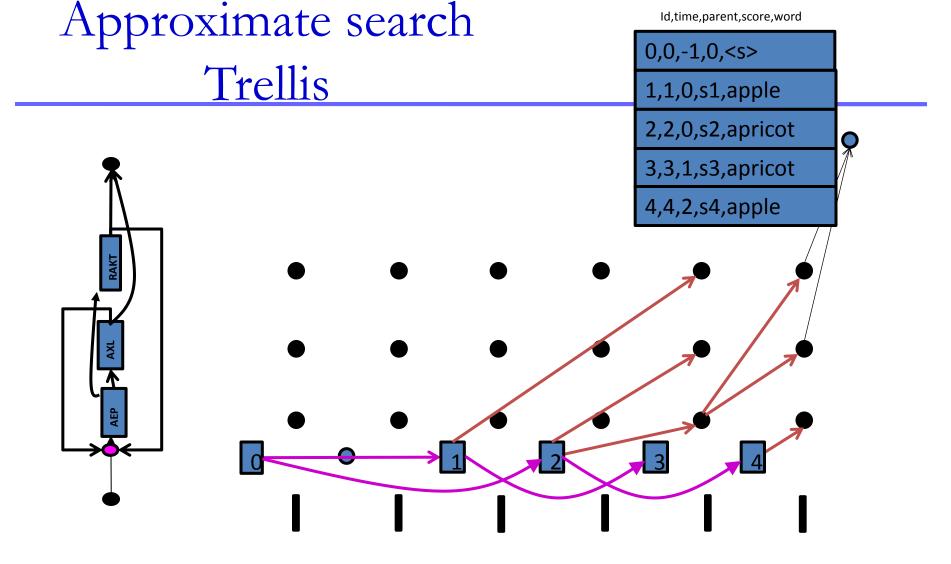
• The winner remains as before



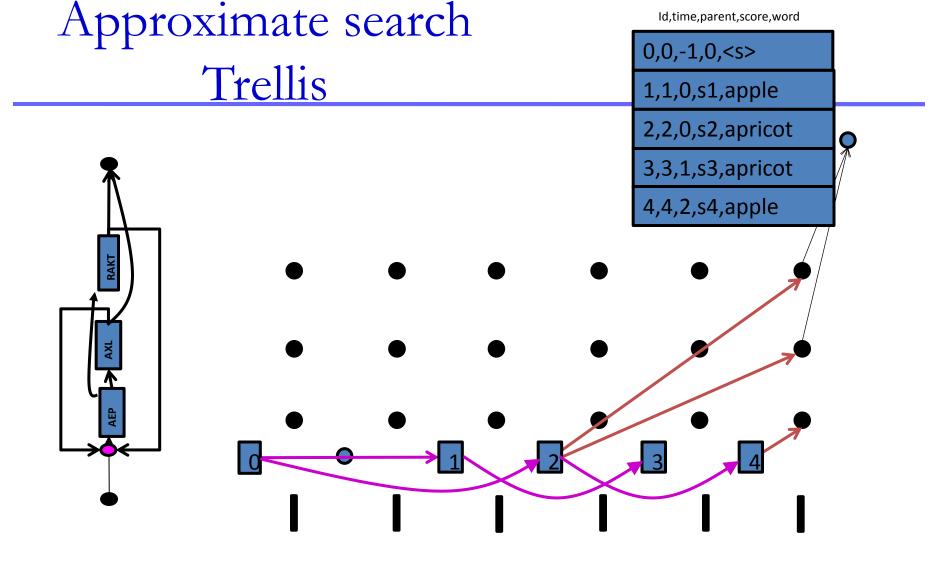
• The winner remains as before



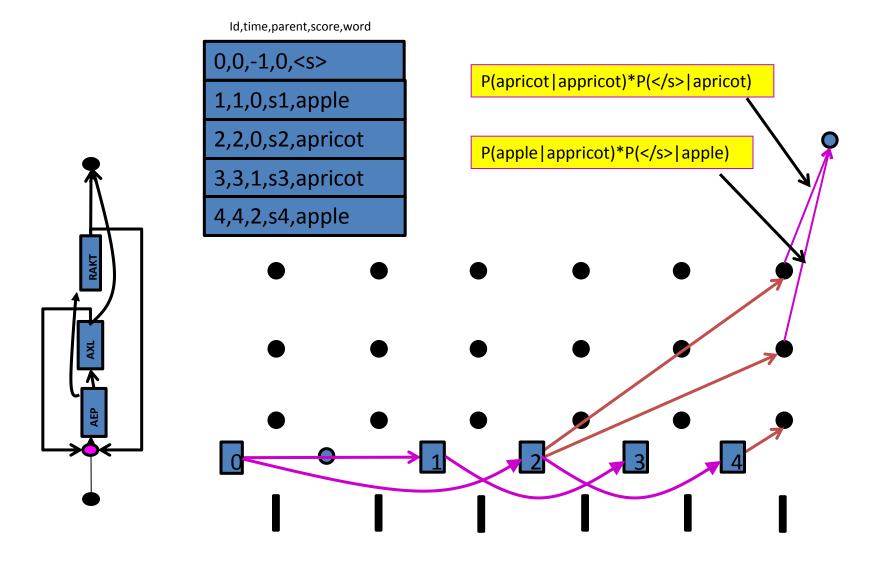
Lets follow this to the end



Lets follow this to the end



Lets follow this to the end

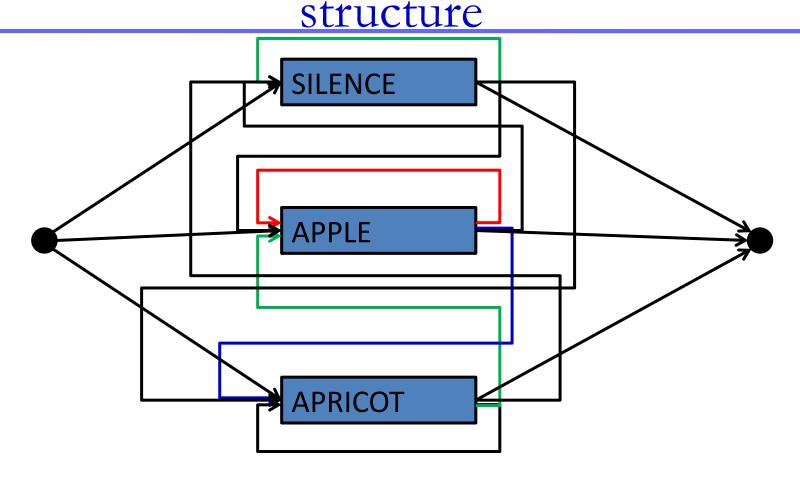


 Note the probabilities being applied to the final transition into sentence ending!

Approximate structures with lextrees

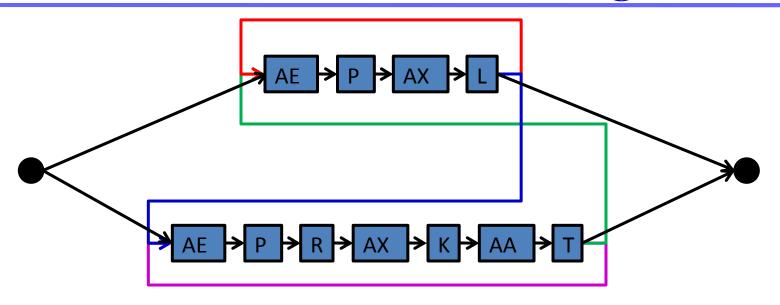
- Can use trigram probabilities instead of bigrams without modifying search strategy
 - Determine previous TWO words and apply appropriate LM trigram probability during search
 - Can in fact handle ANY left-to-right language model
- The approximate structure shown earlier is suboptimal
 - Although highly popular, particularly for embedded systems
- A better approximation is obtained using multiple lextrees
 - Typically 3-5 lextrees
 - The distinction between the lextrees is in the *time* of entry: incoming arcs into the j-th (of K) lextrees only activate if T%K = j
 - i.e. each lextree can be entered only once every K frames
 - Other similar heuristics may be applied
- A still better approximation is obtained using a flat bigram search structure

Approximate decode with flat bigram



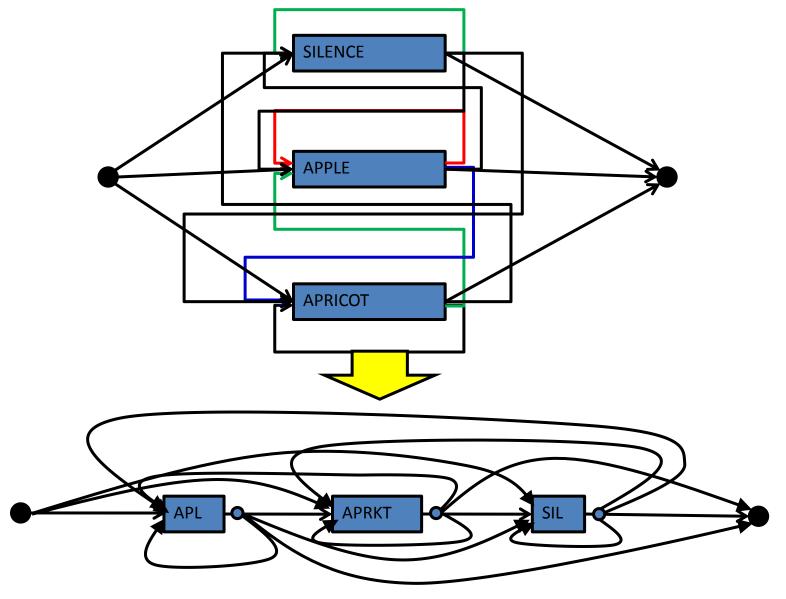
- A better (but more complex) approximate search uses the flat bigram structure shown above
 - Note the manner in which silence is inserted
- Once again, no LM probabilities are introduced at this stage

A closer look at the flat bigram



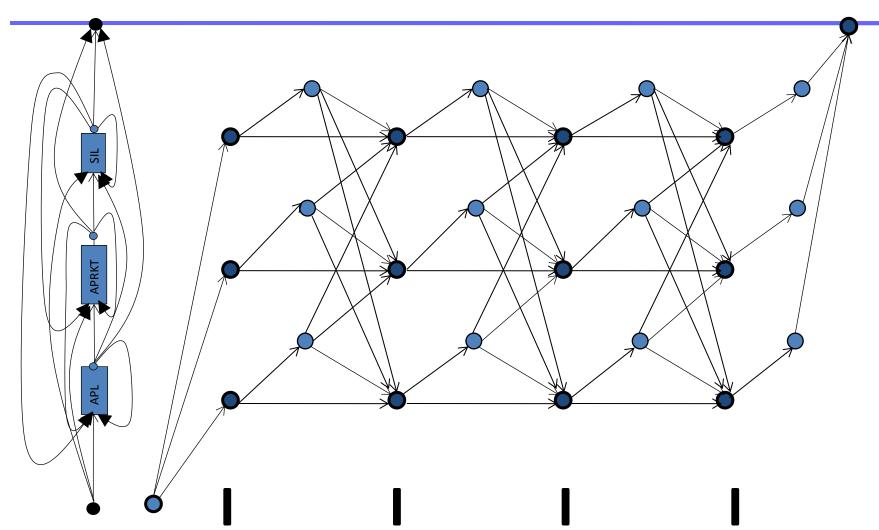
- Not showing silence above to keep it simple
 - But in reality, silence will be included
 - Note: No LM probabilities included
- We take no advantage of the fact that phonemes are shared, however
 - We want to be able to determine word identity at the entry to a word
 - In the following slides we will not show the phonetic breakup of words to keep figures simple

The flat bigram structure



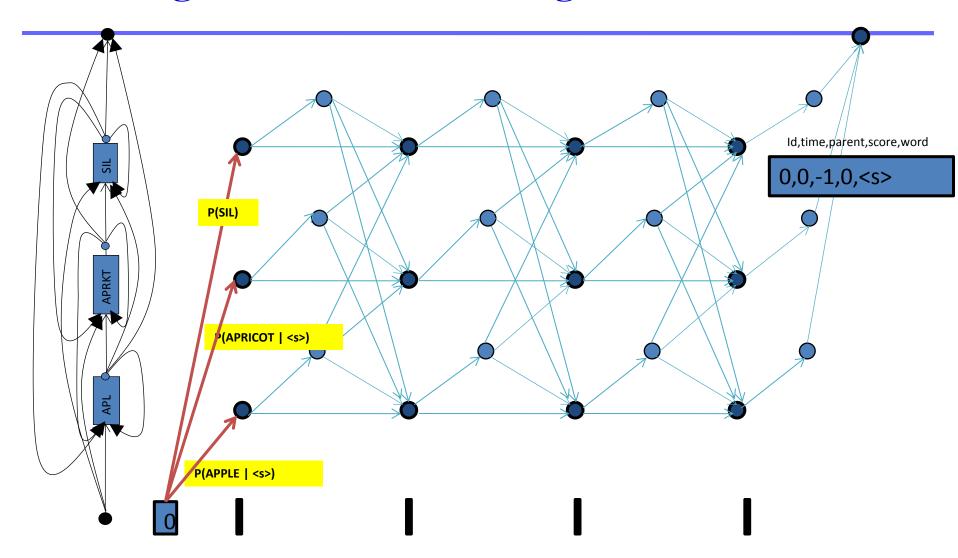
• In the following slides we will assume each word has only one state to simplify illustration

Recognition with flat bigram structure

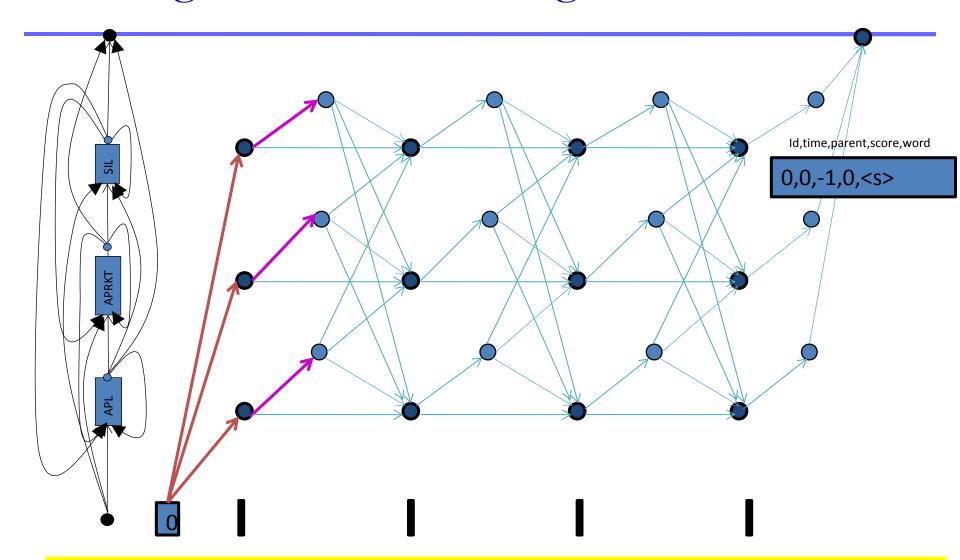


- The trellis is composed as usual
 - But no cross-word language-probabilities are introduced
 - Note: In this form of trellis the non-emitting state at word beginning may be superfluous

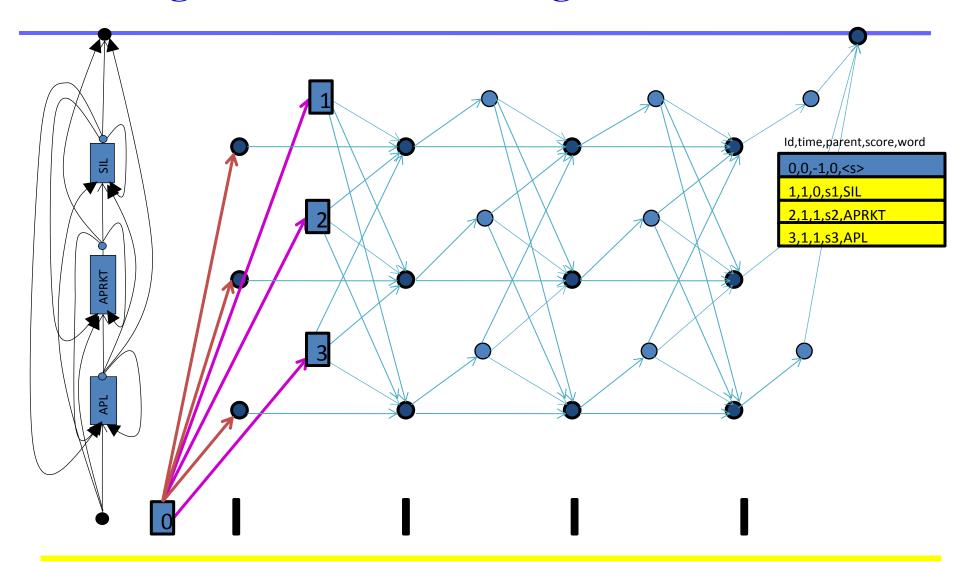
Recognition with flat bigram structure



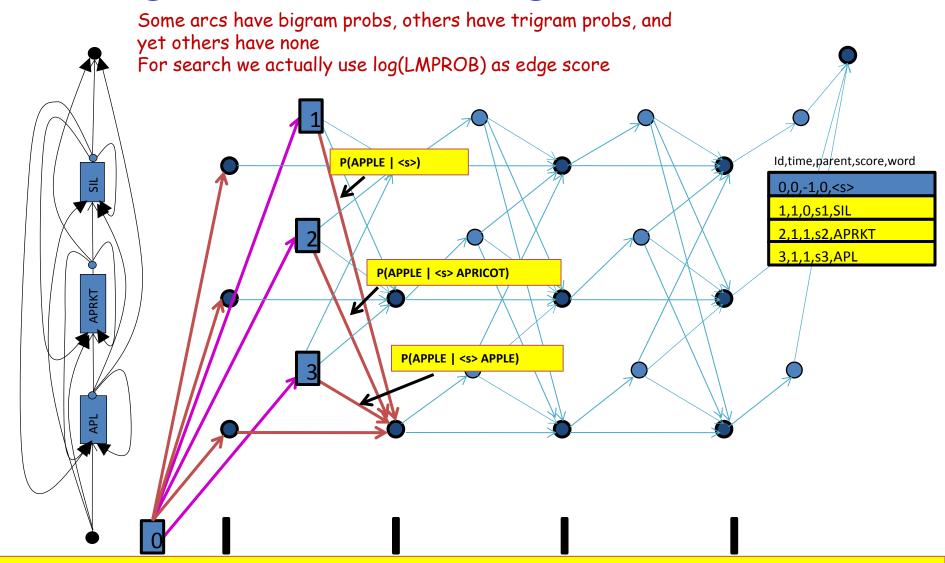
- Bigram probabilities conditioned on start of sentence are applied at the beginning
- Entries to silence carry silence penalty



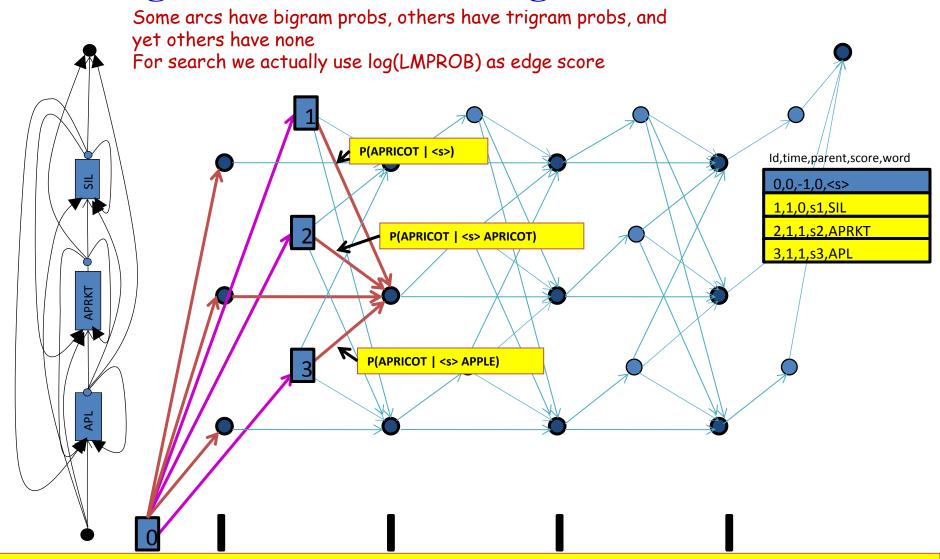
Word ending states move into the backpointer table



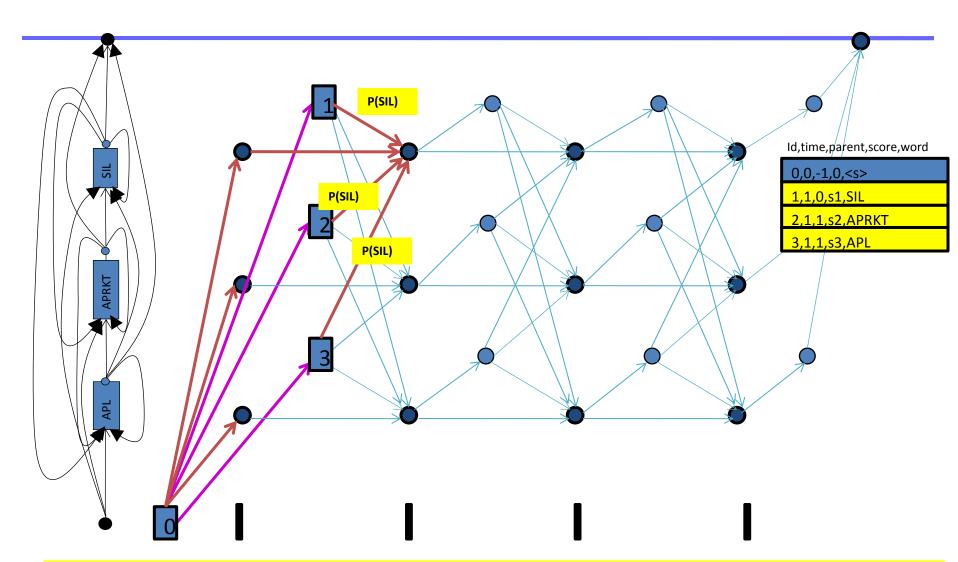
Word ending states move into the backpointer table



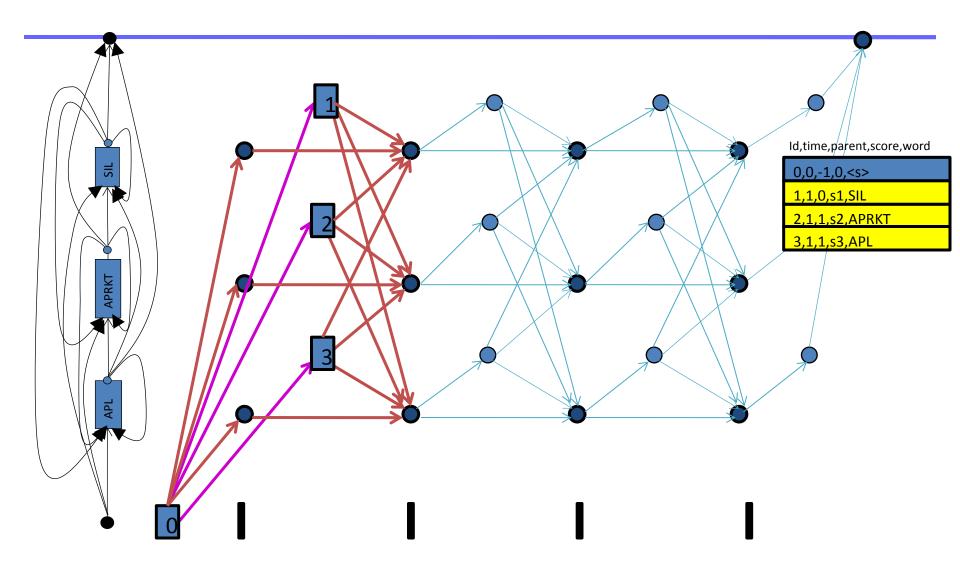
- Note the different LM probability terms applied to the arcs
 - Assuming trigram LM
- The appropriate history to use for the LM probability is obtained from the BPtable



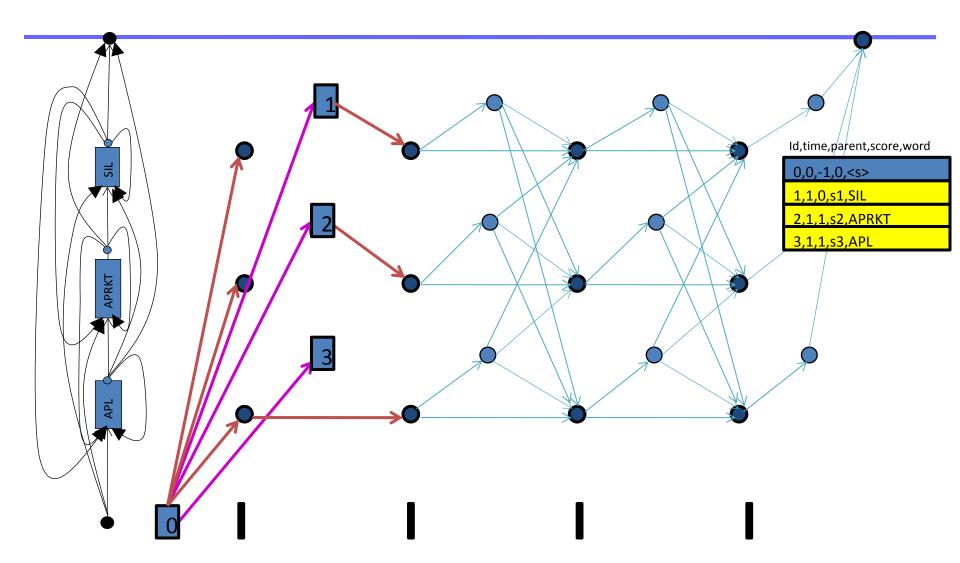
- Note the different LM probability terms applied to the arcs
 - Assuming trigram LM
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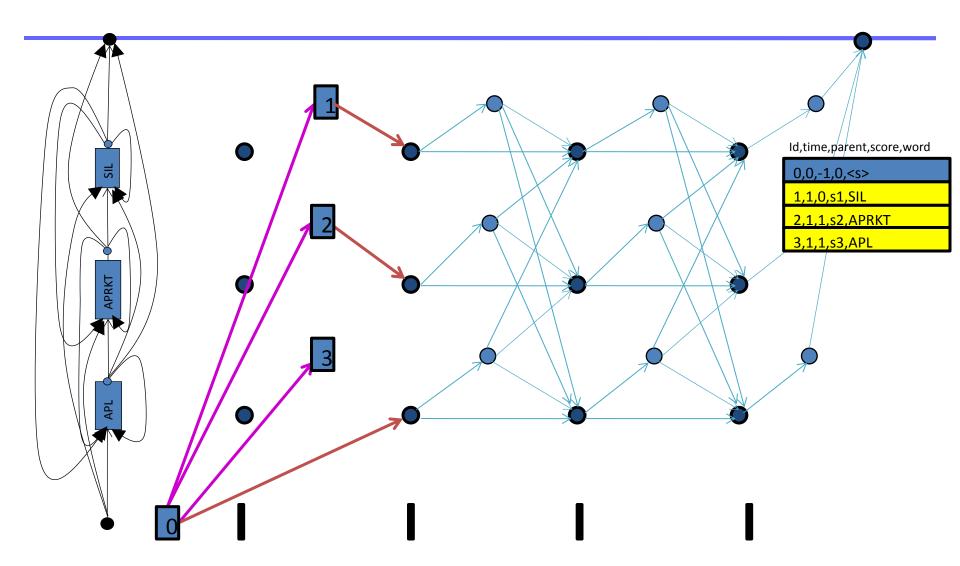
- All cross-word arcs into SILENCE carry the silence penalty
 - Self-transitions within the silence will only carry the self-transition probability for the states of the Silence model



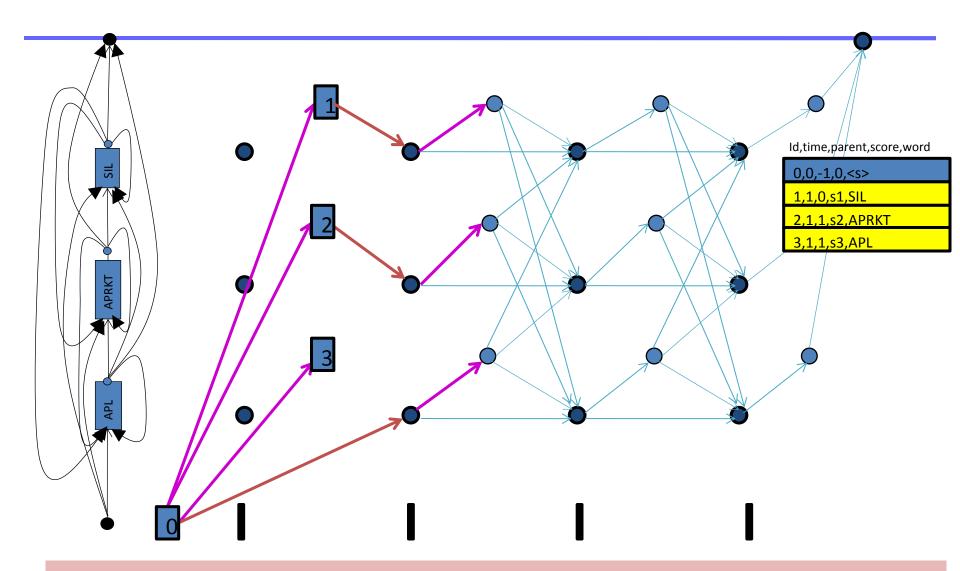
 The actual computation evaluates all of these states in the same timestep



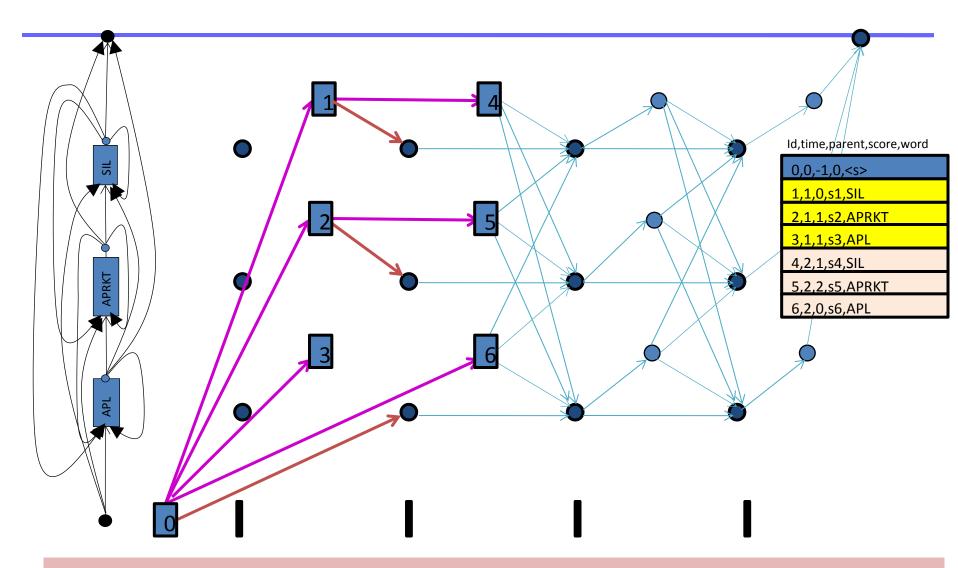
 The actual computation evaluates all of these states in the same timestep



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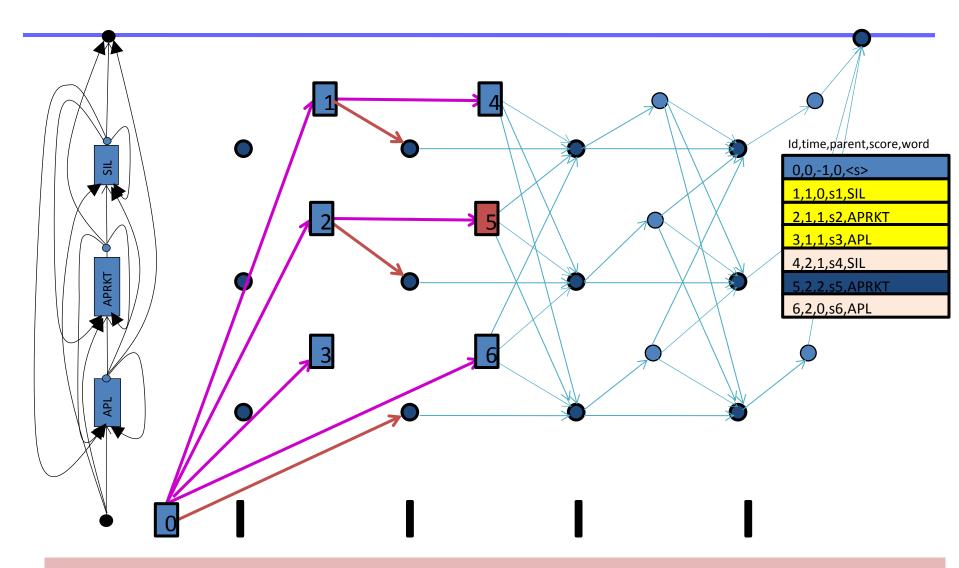
Word ending states move into the BP table



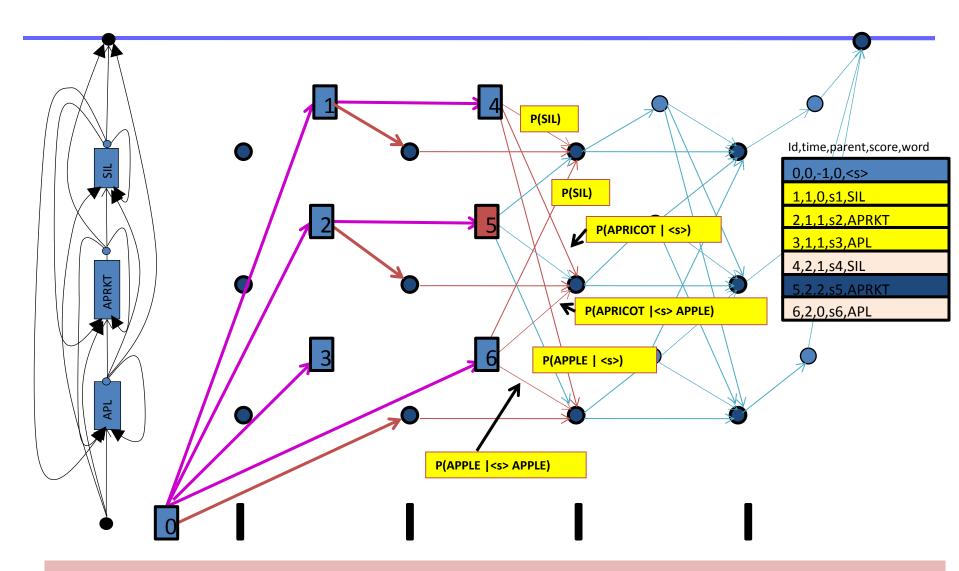
Word ending states move into the BP table

Cross-word Pruning

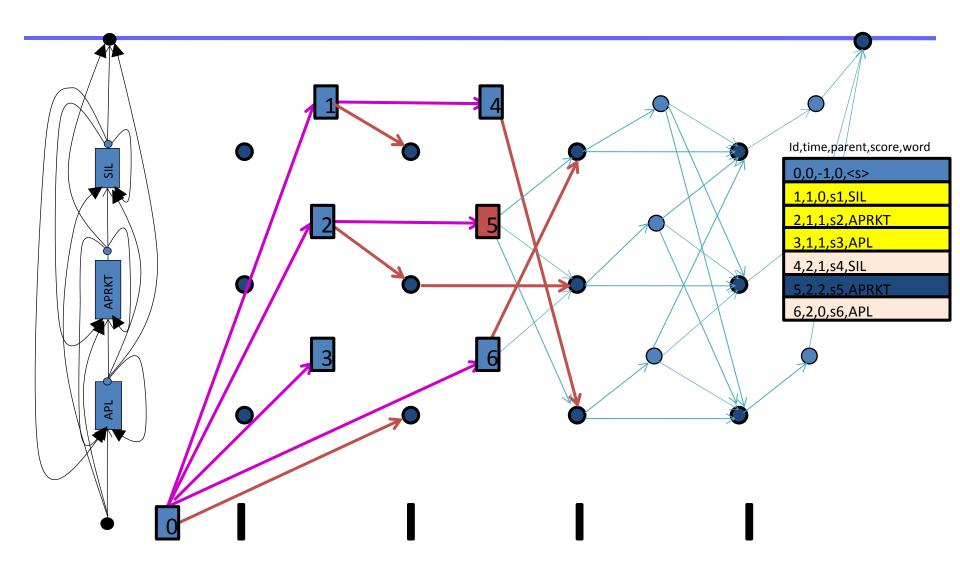
- We can apply a second pruning threshold locally to all entries added to the BP table at a given time
- This is the "new-word beam"
 - This is different from the *state-level beam* applied across all active states at a given time
 - This is only applied to new word terminations
 - A similar new-word beam may also be applied to the approximate lextree and to correct flat and lextree graphs
- In other words, there are TWO different beams we will apply
 - A state-level beam to prune poorly-scoring states
 - A word-level beam to prune poorly-scoring words
- Word beams are typically narrower than state beams



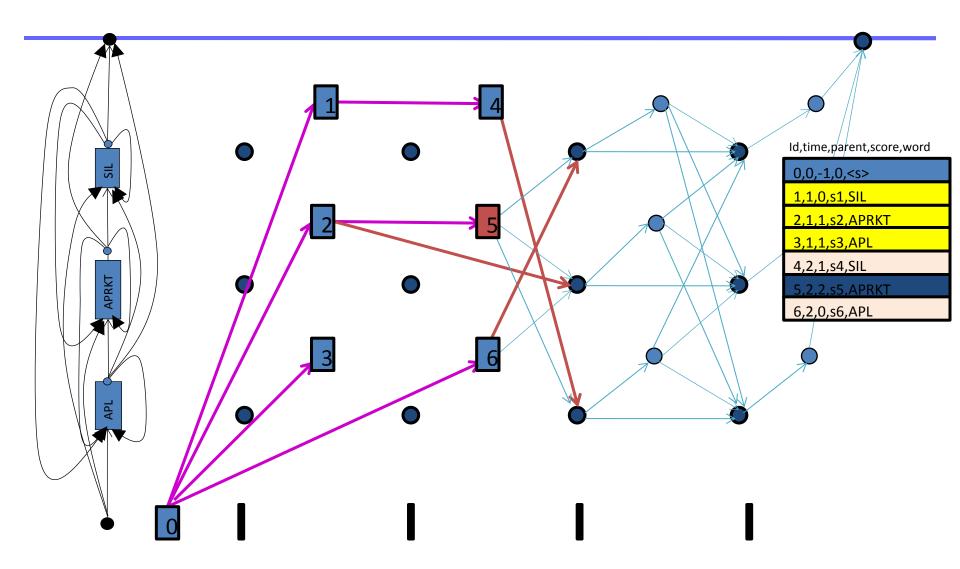
Pruning the word exits



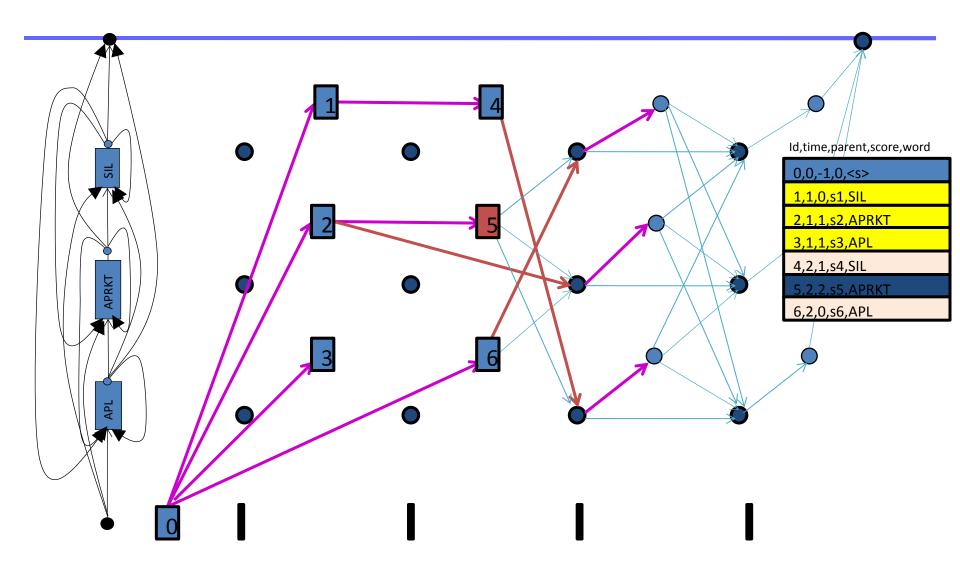
Note the different LM probabilities applied



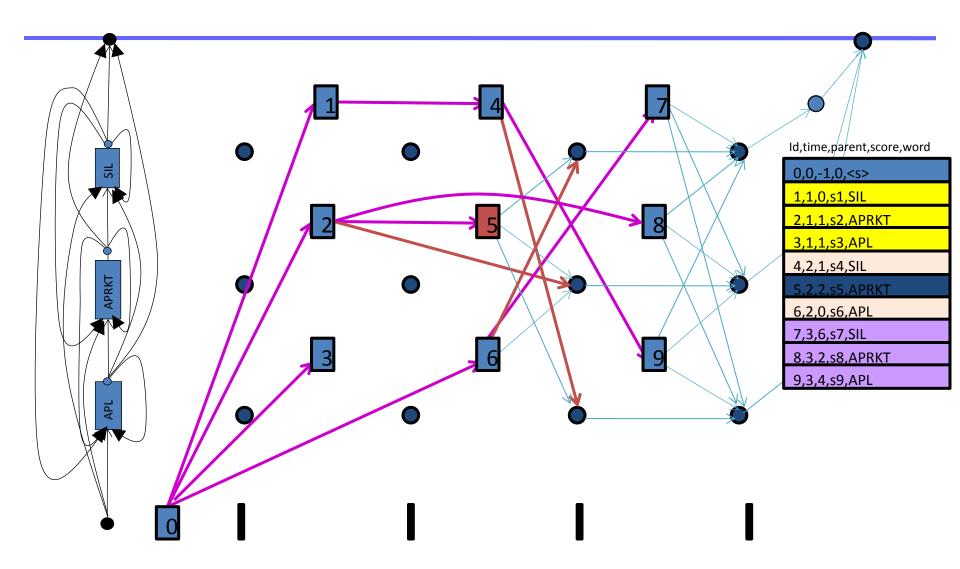
Select the "winner"



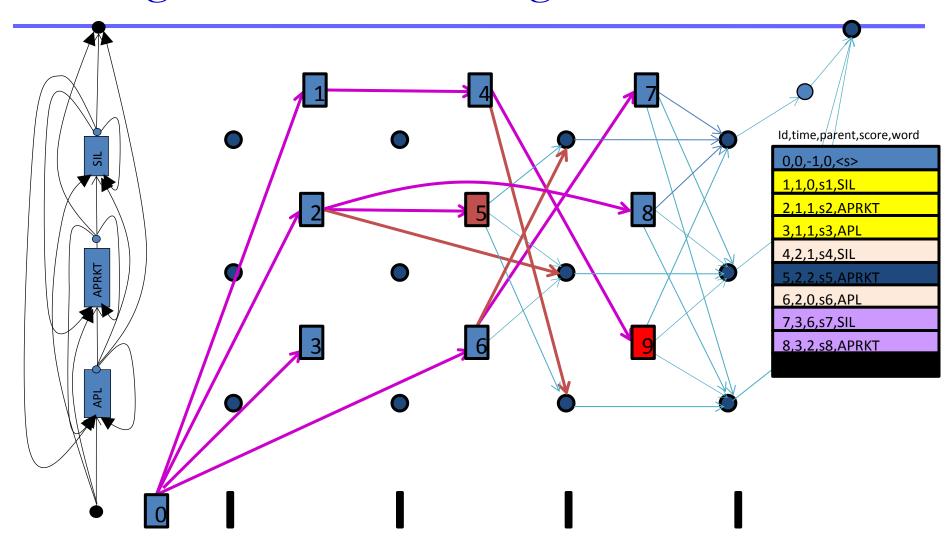
Note the different LM probabilities applied



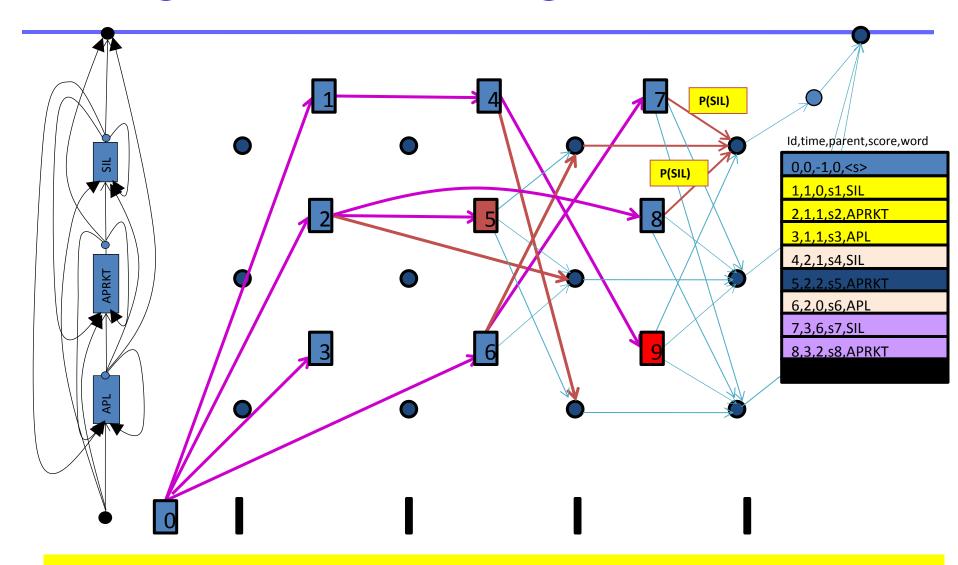
◆ As before, word ending states move into the BP table

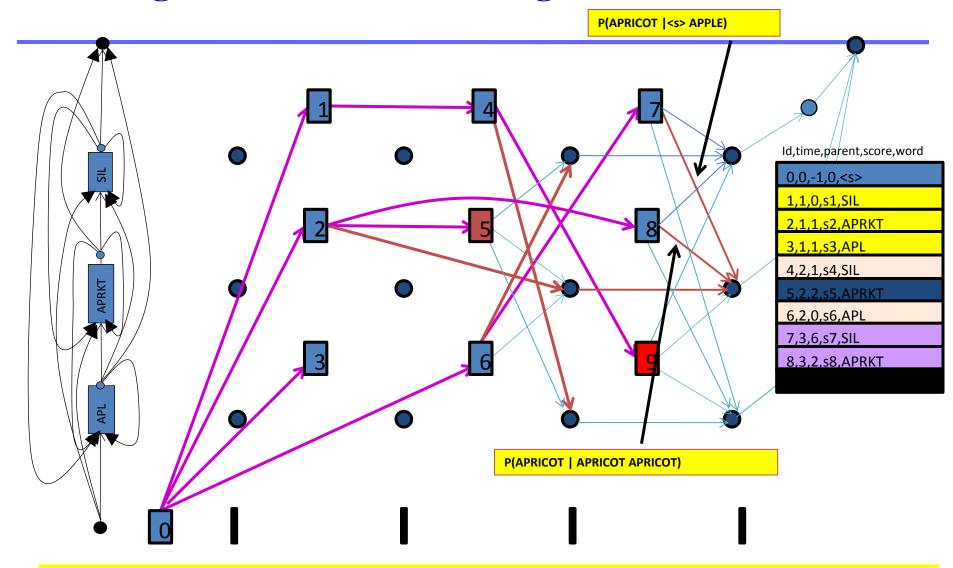


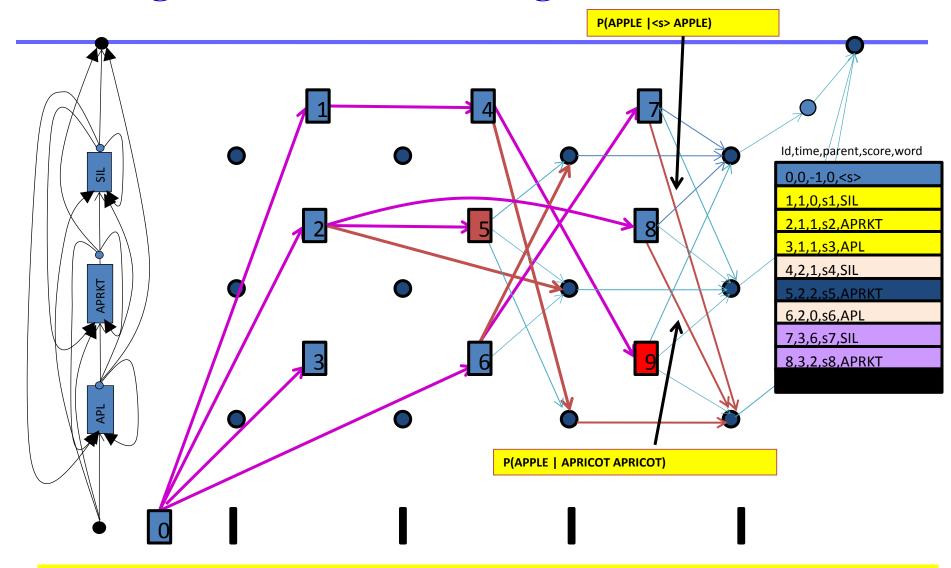
◆ As before, word ending states move into the BP table

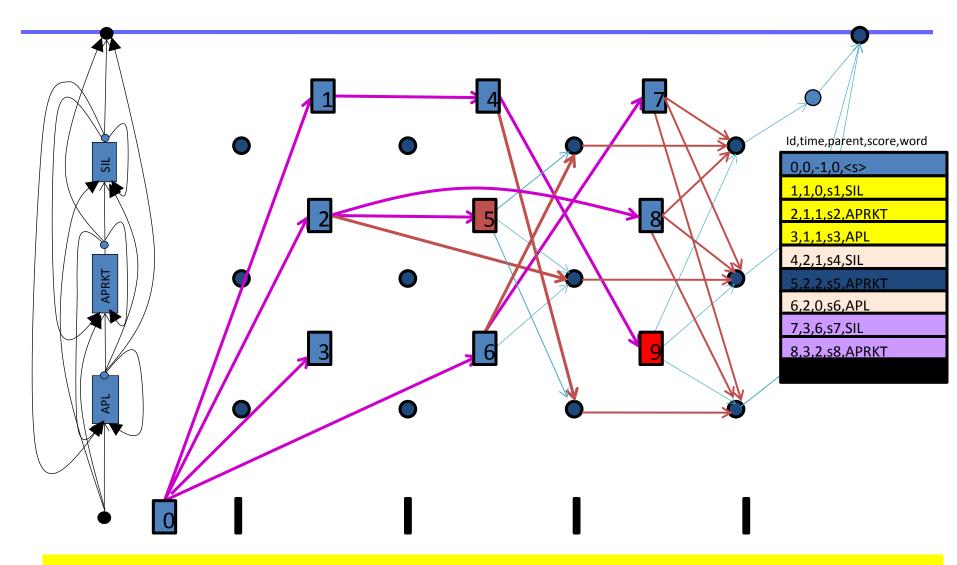


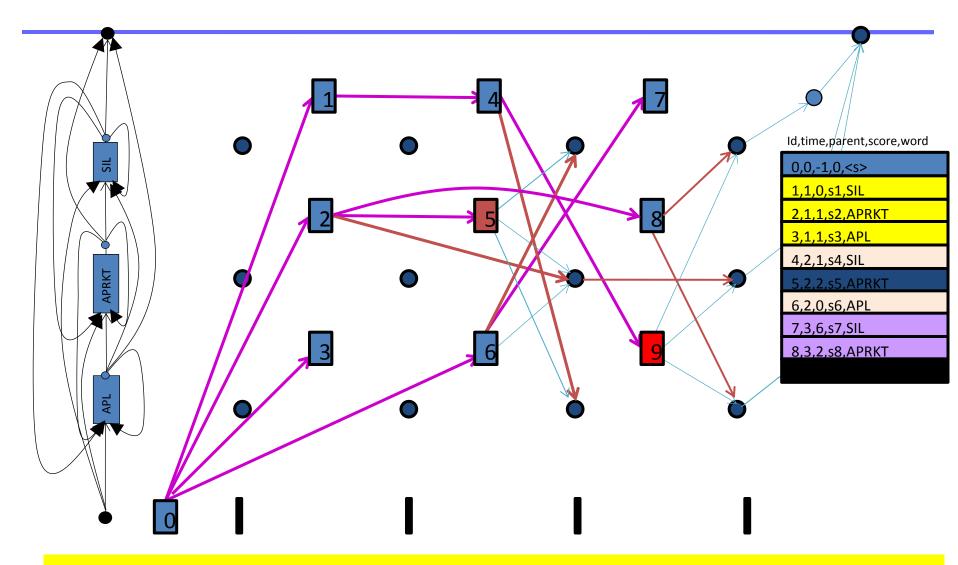
- ◆ As before, word ending states move into the BP table
 - **♦** And are pruned

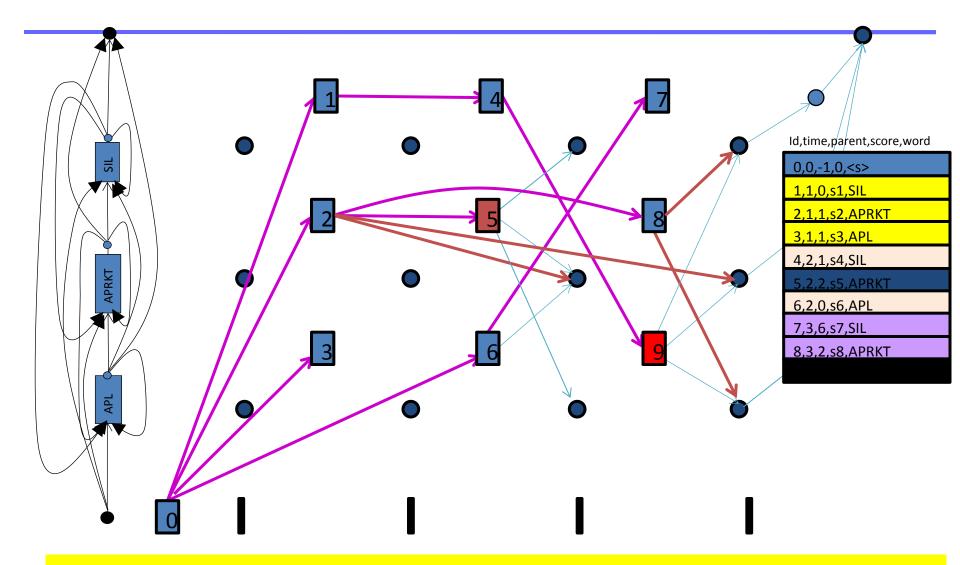


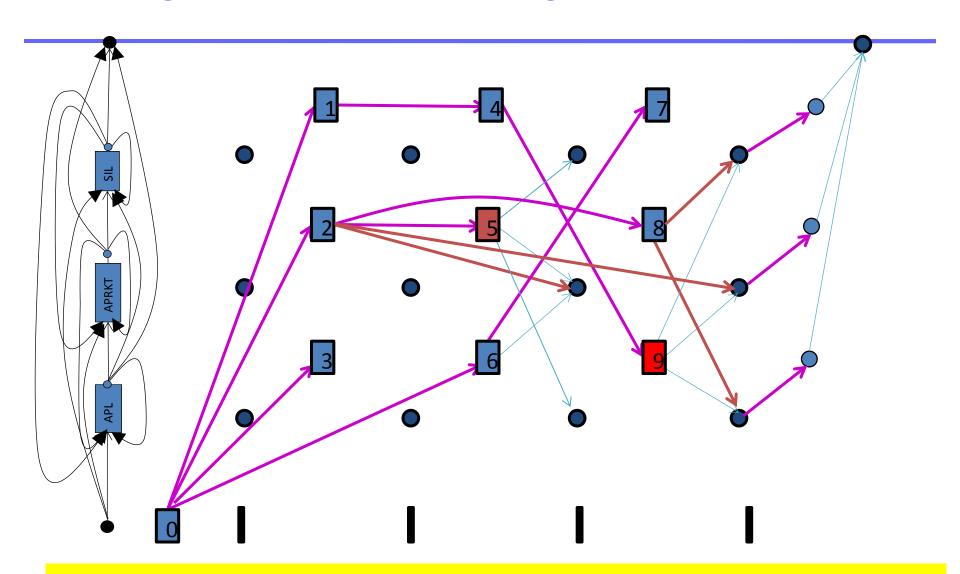




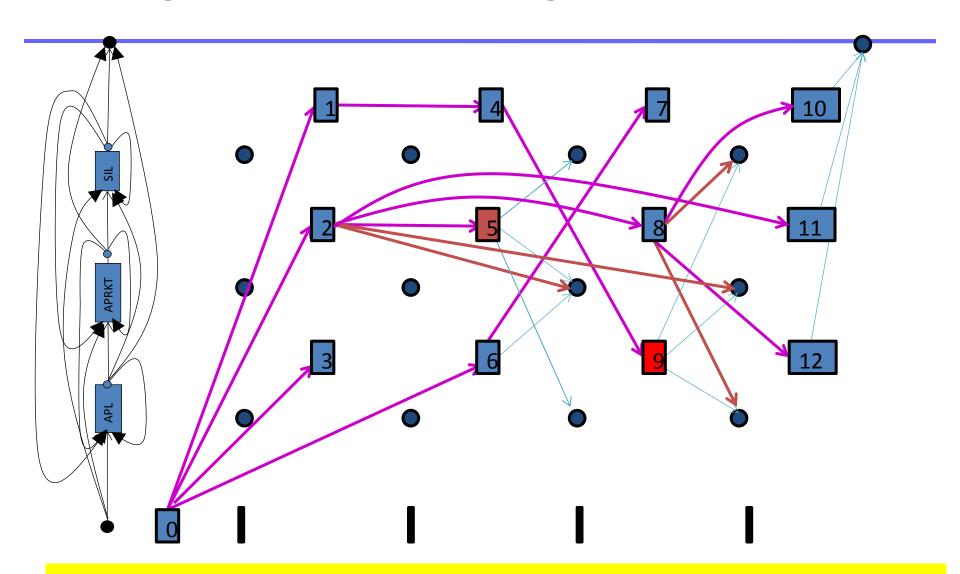




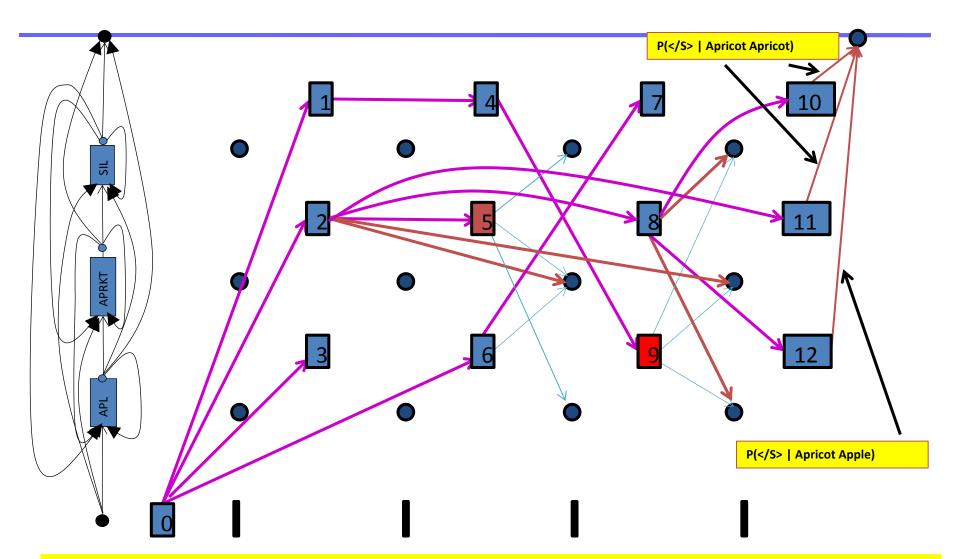




◆ These word exits will end up in the BP table (not shown)



◆ These word exits will end up in the BP table (not shown)



- Note Sentence Ending LM Probabilities Used
 - Note also that multiple hypotheses represent the same word sequence
 - Varying only in the location of silences and word boundaries

Additional Issues

- Several topics left uncovered
- Multi-pass search strategy:
 - The BP table is actually a "lattice"
 - A graph of words
 - Common strategy: compute a lattice using a bigram LM; use that as a grammar/graph for recognition using higher-order N-gram LMs
- N-best hypotheses generation
 - How to search the word graph to generate more than one hypotheses
- Confidence: How to assign a "confidence" score to a hypothesis
 - How much we believe the recognizer's output